# Nactation <br> <br> Tutorial 

 <br> <br> Tutorial}

by Nack Ballard

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$$
\begin{gathered}
\text { Part } 1 \\
\text { Basic } \\
\text { Nactation }
\end{gathered}
$$

## Introduction

The term "Nactation" is an amalgamation of "Nack" (its inventor) and "action notation." Nactation uses terms for actions (run, split, slot...) and directions (up, down...) that are commonly used to convey checker movements.

It takes only a minute or two to learn the five basic characters (illustrated in section 1). Ultimately, you can, if you like, nactate an entire game or match. However, for now, you should regard the following as the primary purpose of Nactation: to describe play sequences and positions that arise in the first few moves of the game.

Imagine that you want to ask someone about the position below, but you have no board or diagram card handy. You want to communicate the position verbally.

You might say: "Okay, suppose you roll an opening 54. You split with the 4 and come down with the 5 . Your opponent responds with a roll of 63 and runs into the outfield. Now you roll 31; how do you play it?"

A shorter way to describe the position is:

## 54-split, 63-run, 31

In written form, single-character Nactation is even shorter. The caption of position \#1, "54S-63R-31," indicates that

Black opened with 54S (54-split), White responded with 63R (63-run), and Black, on roll, has 31 to play.

It is standard to insert hyphens between moves, but slashes, periods, commas or spaces are occasionally seen instead.

Position \#1 is analyzed in detail on page 44 of Backgammon Openings. (To learn more about this book, go to http://www.nackbg.com/bgopreview.htm.)

For all diagrams in this presentation, Black rolled last. If the caption ends with only the roll (e.g., "31"), it is Black to play. If the caption ends with the roll and another character (e.g., "31P"), Black has just completed his move. The text will clarify as well.

Positions in this tutorial are designed to teach not only Nactation but also expert checker play by example. Moves in the (captioned) lead-up sequences are usually best and always "well played"-giving up no more than .02 in equity. In the text, candidate moves are often helpfully described, for example as "best" or "better than" or "a common mistake," etc., and for all positions you can look up rollout results in section 17.

In the darkly shaded column to the left of the text area of this document, click on the top icon. "Page thumbnails" provides you with an easy way to instantly jump to any page (though this tutorial is not actually cross-referenced by page number).

Now click on the second icon ("Bookmarks"), which displays three sub-icons. Click on + to expand, - to diminish. "Part 1" and "Part 2" let you navigate by section number, and "Nactations" by character segment. (To adjust the width of the column, drag the border or click on the right arrow at the top; and to restore, use the left arrow.)

A basic knowledge of Nactation will help you follow or join discussions in online forums and better comprehend some articles.

Nactation is NOT an all-or-nothing proposition. As you learn new letters, you can gradually substitute them in. Even learning a mere handful of letters and continuing to use longhand (traditional notation) for all or part of the other moves will noticeably reduce your amount of writing or typing.

Section 1 explains most of what you need to know to use Nactation. Later sections will help you refine your usage (if you so choose).

## Section 1: Basic Characters

Nactation letters are easy to learn. In modern backgammon, the opening move is almost always one of the following types:

$$
\begin{aligned}
& \mathbf{D}=\text { Down } \\
& \mathbf{P}=\text { Point } \\
& \mathbf{R}=\text { Run } \\
& \$=\text { Slot } \\
& \mathbf{S}=\text { Split }
\end{aligned}
$$

I'll define these terms in alphabetical order.

Dstands for Down. It typically refers to playing from the midpoint to the outer board, and usually with two checkers.

For example, in position \#2, White played 52D (or 52-down).

In the same position (\#2), Black responded with 43D (or 43-down).

\# 2 52D-43D

\# 3 61P-63R second letters in "Slot" overlap to form the $\$$ symbol.

Classically, "slot" refers to playing a checker to a vacant offensive point (usually a high inner board point).

Nactation adds a meaning that refers to the entire move. You "slot" by playing a checker down and putting it or another checker onto a vacant offensive point.

In pos. \#4, White played 21\$ (or 21-slot).
In the same position (\#4), Black replied with 62\$ (or 62-slot).

Smeans Split. The traditional definition is to break an anchor.

With Nactation, Split is a two-part move. It means: (1) to play a checker anywhere on the far side of the board, and (2) to play down from the opponent's outer board (typically from the midpoint).

In pos. \#5, White played 43S (or 43-split).


In the same position, Black replied with 52S (or 52-split).

You are now ready to use Nactation: the above five letters/symbols cover most early game situations. For practice, write down all the opening moves you know in three columns: (1) the roll, (2) the traditional notation (if you know it), and (3) the Nactation letter.

For example:

| Roll |  | Notation |  |
| :---: | :---: | :---: | :---: |
|  |  | Nactation |  |
| 61 |  | $13 / 7,8 / 7$ |  |
| 64 |  | $24 / 18,13 / 9$ |  |
| 32 |  | P |  |
| $32 / 11,13 / 10$ |  | D |  |

If and when you would like to learn additional letters, move on to section 2.

## Section 2: Other Useful Letters

Z
stands for reverse split (or whimsically, "Zplit"). If you write an " S " backwards (or reflect it in a mirror), it resembles a "Z."

You can use Z for a splitting move in which a back checker plays the smaller number, and the larger number is played down from the far outer board.

In position \#6, White played 43Z, moving the back checker with the smaller number (the 3).

Compare with the previous position. In \#5, White played 43S. In \#6, she played 43Z.

In position \#6, Black responded with 51S. You may call this move 51Z, though it is unnecessary. Black could not legally split with the large number (the 5) nor come down with the small number (the 1 ).

Convenience clause (defined above \#62): The idea is that for an initial splitting move where the roll contains a 5 and/or a 1 (e.g., Black's move in \#5 or \#6), you can use "S" unambiguously; indeed, I prefer it because it more instantly suggests the word "Split."

Ustands for Up (as in moving $u p$ to meet the enemy forces). It refers to advancing back checker(s), up to and including to the opponent's bar point. (If any farther, it qualifies as R , a running move).

In position \#7, Black played 43U.
The subtleties of $U$ are discussed in detail under "V," starting with position \#18.

\# 7 51S-43U

The next three related letters ( $\mathrm{H}, \mathrm{X}$ and K ) are very descriptive and handy. stands for Hit loose (and only once).


In \#8 above, Black can hit inside with the deuce. If he comes down with the 3, as in 8.1 (below, left), the move is nactated $\mathbf{3 2 H}$. The gist of the "down clause" (more fully explained above \#67) is that you play down for a non-hitting portion of an H move.
[If Black rolls 62 in $\# 8$, using the entire roll to hit in the outfield is 62 H . The alternative that hits inside with the 2 and brings down the 6 is 62 . Refer to section 10 and \#67.]

Xhas two diagonal strokes that represent hit and split. (Some may prefer to think of X as "eXpel and split," or even, whimsically, "Xplit"). An X move hits on the near side with one number and plays on the far side with the other number.

With the roll of 32 in position \#8 (above), Black has a strong alternative: to hit with the 2 and split with the 3 . This move, shown in 8.2 (below, middle) is nactated 32 X .

stands for Kill, and it means to hit two checkers.

With the roll of 32 in position \#8, Black's third (though distinctly inferior) choice is to hit twice. This move, shown in 8.3 (below, right), is nactated 32K.


Having finished section 2, you should be able to nactate virtually any second or third roll situation except for those involving doublets.

Here is a recommended drill: Set up a backgammon board with the opening position. Roll one die for yourself and one die for your imaginary opponent.

Whoever has the higher die plays the opening roll. Make what you consider to be a strong move, and say the Nactation letter aloud. Then roll for the other player (if you roll a doublet, ignore and reroll), make a move and announce the letter.

After two rolls (one roll for each player), start over with the opening position and repeat the procedure. If you re-encounter an opening roll or reply situation, try to vary your move if there is a reasonable alternative. (If you feel confident, you can continue to a third or fourth roll in the sequence before starting over with the opening position.)

If you are not sure what letter to use for a move, look for the relevant discussion in section 1 or 2.

If and when you are ready to add doublets to your repertoire, move on to section 3 .

## Section 3: BEACON for Doublets

Nactating doublets will save you a lot of writing or typing. Diagram 77.1 provides a nice example: "Bar/21 24/20 13/9 11/7*" (23 keystrokes) is reduced to "B" (1 keystroke).

This section defines and explains the letters used for doublets, where the parts of the move are played as two separate pairs.

To help you remember these six letters, I am presenting them in the order of BEACON. This happens to rank them from most to least commonly arising, except for N .

Bstands for Both. It means playing Both on the far side (i.e., with back checkers) and near side (specifically to or within the outer board) on the same move.

Position \#9 shows 44B. This balanced move gives Black a big advantage right out of the starting gate.

B is the most common move with double $6 s, 4 s$ and 3 s in the early game.

\# 9 51S-44B

\# 10 54D-22E

Astands for Attack. Half the roll is played to and the other half within the inner board.

In position \#11, Black played 55A.
If Black had instead rolled double 3s, he could also have made two inside points (pointing on a different blot) with 33A.

In \#9 (earlier diagram), Black could have made two inside points with 44A (instead of 44B), the move most likely to win a gammon. [See rollout \#9 (g), section 17.]

A is not always an Attacking (or Aggressive) move. What distinguishes A is the source and destination quadrants: outer-to-inner, and inner-to-inner.

stands for Cross, where the near-side half of the move Crosses the bar. The other half advances the back checkers.

In position \#12, Black played 33C.

0
stands for Outer. Half of the move is played into (or within) a player's Outer board and the other half is played out of his Outer board.

In position \#13, Black played 660.

\# 11 54S-55A

\# 12 41\$-33C

\# 13 61P-660
stands for Near. The move is divided between the two Near-side quadrants (from the perspective of the player making the move).

Half of the move is played to or within the outer board (frequently from the midpoint). The other half is played entirely within the inner board.

For 22N, 33N, 44N and 55N, a player brings two checkers down and uses two inside spares to make a new point.

11 N , shown in \#14, is the only N move as early as the second roll of the game that plays no checkers off the midpoint.

\# 14 64R-11N

The above six positions demonstrate examples of simple doublets: those played in pairs. (Complex doublets are covered in sections 15 and 16.)

Congratulations! You now know the main letters for both doublets and non-doublets.

I recommend that you repeat the interactive drill described at the end of section 2, but this time include doublets. As you make each move, announce the Nactation letter for mental reinforcement.

The next few sections will add to your arsenal for nactating third and fourth roll moves.
[Henceforth, captions of after-diagrams will supply only Black's last roll + move instead of the entire sequence (e.g., "...31E" instead of $51 \$-51 \$-31 \mathrm{E}$, for 15.1 ). In the text, a move will usually be referred to in the standard manner: simply by its letter without restating the roll (e.g., "E" instead of 31E).]

## Section 4: BEACON for Non-doublets

BEACON letters can also be applied to non-doublets.

\# 15 51\$-51\$-31

In \#15, Black's roll of 31 offers three close moves. One option is to split with the 3 and cover with the 1, shown in 15.1 (below, left) and nactated E. Black plays half of his roll in Each inner board, much in the same way he did in \#10. (See also 31.3, 53.1 and 57.1.)

Black's second option is $\mathbf{N}$, dividing the roll between his Near side quadrants. Half the move is played to his outer board ( 3 down) and the other half within his inner board (the 1 covers), shown in 15.2. In that sense, it resembles his N move in \#14. (See also 53.3.)

Black's third reasonable alternative is to play both the 3 and 1 to the same point, covering the inside blot: shown in 15.3 (below, right) and nactated $\mathbf{A}$. Black plays half of his roll into and the other half within the inner board; in that sense it is an Attacking (or Aggressive) move similar to his doublets move in \#11. (See also 16.3 and 53.5.)

15.1 ...31E

15.2
...31N

15.3 ...31A


In position \#16, Black rolled 32. (Hitting is a blunder, both here and in \#15.)

In 16.1 (below, left), Black brought the 2 down and covered with the 3 . He played both into and out of the Outer board: the move is therefore nactated $\mathbf{O}$. (Compare to \#13.)

In 16.2 (below, middle), Black covered with the 3 (Crossing the bar) and split with the 2. This move is nactated C. (Compare to \#12.) Similarly, from the large diagram \#15, covering with the 3 and splitting with the 1 (fourth best) would have been C .

Black's third good alternative in \#16 is to cover with the 3 and slot inside with the 2, shown in 16.3 (below, right), and nactated $\mathbf{A}$ for Attack or Aggress. For both positions \#15 and \#16, A is a close move but third best.


I have saved B for last because of its unusual application. If non-doublet B were simply a half-sized version of doublet B (see \#9), it would perform the same function as either S (see \#5) or Z (see \#6). It is not and does not.

Instead, to better divide the labor, non-doublet B refers to (Both) moving one checker on the far side and the other checker within the outer board (instead of into the outer board -i.e., from the opponent's outer board, as S or Z handles).


Consider \#17 (above). With a roll of 21 or 61, Black should split his back checkers with the 2 or 6 , and button up a point in his outer board with the 1 . The position after Black plays 21B is shown in 17 x (below, left); the position after 61B is shown in 17 y .


For an apt comparison of (non-doublet) B, S and Z moves, see position \#62.

## Section 5: Areal Letters

There are two types of Nactation characters: style and areal.
Style characters include both letters and symbols. The most basic—P, \$, H, X and K— were defined in sections 1 and 2 . More style characters will appear in sections 6 and 7 .

The majority of Nactation characters are areal (i.e., area-based). This group consists entirely of letters (no symbols), and can be applied whether or not they hit, make or break points, or create or safety blots. Areal letters operate purely by areas of the board where checkers are moved, and-depending on the number of these movement areascan be uni-areal, bi-areal or multi-areal.

Most of the letters you have seen up to this point are bi-areal: they focus on exactly two movement areas of the board. This subgroup is made up of $\mathrm{S}, \mathrm{Z}$ and the BEACON letters.

D, R and U (see \#2, \#4, and \#7) are uni-areal: each operates in only one movement area of the board. Here, in section 5, the remaining three uni-areal letters (V, J and I) are introduced, and at the end of the section is an overview of the uni- and bi-areal letters.
is a Variant Up. (For Up, see "U" explained in \#7). Note that V follows U in the alphabet and physically resembles it.


$$
\text { \# } 18 \text { 41S-42P-21P-21 }
$$

In \#18 above, Black has rolled 21. If he brings up one back checker, as shown in 18.1 (below, left), the move is nactated U. If instead he brings up both back checkers (as shown in 18.2), the move is nactated $\mathbf{V}$.


Is one to infer, then, that U refers to playing one checker up, while V refers to playing two checkers up? No, not at all! The next two examples will help clarify.


In position \#19 (above), Black rolls 21. If he moves the leading back checker 3 pips, he has played $\mathbf{U}$, shown in 19.1 (below, left). By contrast, if he moves the trailing checker 3 pips, he has played V, shown in 19.2 (below, right). Both moves bring one checker up.


\# 20 51\$-43S-42

In position \#20 (above), Black rolls 42. The (best) candidate of entering with the 2 and coming up with the 4 is U, shown in 20.1 (below, left). Entering with the 4 and coming up with the 2 is V, shown in 20.2 (right). Both moves bring two checkers up.


In short, if there is only one legal up move with the roll, use U . If there are two, the move that plays the lead back checker closest to home is nactated U , and the other move is V . (This guideline may be overridden when an up move hits or anchors; e.g., \#47 and \#48.)

U and V are married; they are the top two members of the U "family." Every other letter has its own distinct family. The concept of a family is expounded in sections 10 and 14.


In position \#21 (above, left), Black rolled 63. His safest (and best) move is to cover his blot and slot (as shown in 21.1), thereby Jumping two checkers over the bar with J.

As has just been explained, for non-doublets the uni-areal letter J means that both portions of the roll Jump over the bar. For a doublets roll, all four portions Jump:


In position \#22 above, Black's best move is to Jump all four checkers over the bar with J, as shown in 22.1 (below, left). In this way, he makes his strongest three-point board.

The (very close but) second best move is A, shown in 22.2 (below, right). See also \#11.

stands for Inside. It refers to playing one or more checkers entirely inside (within the inner board).


Position \#23 above is similar to a position analyzed on page 28 of Backgammon Openings (http://www.nackbg.com/bgopreview.htm). With his roll of 31, Black should cover his inner board blot and hit, as shown in 23.1. This Inside move is nactated I.

The hit here is incidental. Do not confuse Black's 31 I in 23.1 with his 31 A in 15.3. There is only one source quadrant (inner board) for I, whereas there are two for A.

As by now you might have surmised: When applying I to a roll of doublets, all four portions of the move are played Inside. For example:


In \#24 (left), Black should play all four deuces Inside with I, as shown in 24.1 (right), rather than anchor or hit outside. Such a committal choice may cause a positional player of the 1970s to roll over in his grave, but the swing is huge if White fans or rolls a 6 .

## Areal Overview

Not all areas of the backgammon board are utilized equally. Given that 13 of the 15 checkers start on the midpoint or lower in the opening position, there is a concentration of moves on the near side of the board. For this reason, of the four areas of movement (on which Nactation's areal concept is based), only one is defined by destinations on the far side of the board. The other three involve checker destinations on the near side.

Every backgammon move is composed of either two portions (if the roll is non-doublets) or four portions (if the roll is doublets). Each "portion" (sub-move) of the move performs one of four basic checker movements (which can be used as nouns):
$\mathbf{R} \mathbf{u n} \quad$ on the far side of the board D own to $^{\text {to }}$ within the outer board J ump from outer to inner board I nside within the inner board

It is the specific way in which a move's two or four areal movements are combined that determine which areal letter is appropriate.

If both or all four portions are played in the same area, then just use the uni-areal letter: R (which is U in some cases), D, J or I. For example, R is composed of two or four "runs."

When half of the move is played in one area and half in another (a $2: 2$ ratio for doublets or $1: 1$ for non-doublets), the uni-areal letters of JIRD (i.e., RDJI) are the parents, and the bi-areal letters of BEACON (introduced in sections 3-4) are the offspring-the hybrids.

In the board illustration below, the parents have big letters and the hybrids small letters. Each hybrid is positioned equidistantly between its parents.

## R



For example, if half the move is played Down (D) and half Jumps over the bar (J), then-areally speaking-D and J have each contributed half the move, thereby producing the hybrid Outer ( O ). You can write this as $\mathrm{D}+\mathrm{J}=\mathrm{O}$. Below are all six combinations.

$$
\begin{array}{ll}
\mathbf{R}+\mathbf{D}=\mathbf{B}(\text { or } \mathrm{S} \text { or } \mathrm{Z}) & \# 5-6, \# 9, \# 17,39.3, \# 51-52, \# 54-56, \# 60, \# 62 \\
\mathbf{R}+\mathbf{I}=\mathbf{E} & \# 10,15.1,31.3,39.2,53.1,57.1,60.3 \\
\mathbf{J}+\mathbf{I}=\mathbf{A} & \# 11,15.3,16.3,22.2,39.4,53.5,55.2 \\
\mathbf{R}+\mathbf{J}=\mathbf{C} & \# 12,16.2,39.1,60.2 \\
\mathbf{D}+\mathbf{J}=\mathbf{O} & \# 13,16.1,81.1 \\
\mathbf{D}+\mathbf{I}=\mathbf{N} & \# 14,15.2,53.3
\end{array}
$$

For doublets, it is also possible to play three portions in one area and one in another, or to play portions multi-areally (i.e., in three or four areas). Areal letter families for all possible doublet moves are precisely defined and illustrated in sections 15-16.

## Section 6: Style Letters

The previous section explains the areal concept. Areal letters are indispensable; they provide a guaranteed way of nactating a move that lacks an obvious action word to describe it or simultaneously achieves more than one objective. Moreover, the use of areal letters in conjunction with the "hit-more-6 rule" (the way to distinguish between two or more moves that use the same letter), as outlined in section 10 , is the most reliable way for skilled nactators to communicate with each other or with a computer program.

Any backgammon move from any position can be described by an areal letter. Strictly speaking, therefore, style characters are unnecessary; moreover, they are more difficult to use perfectly. (Due to a less natural fit with the hit-more-6 rule, an extra clause or convention is sometimes substituted or added.) Well, then-why use them?

Here are some reasons that style characters are worthwhile:

- Given that they relate to action words, style characters are among the easiest for inexperienced nactators to grab out of the air.
- The interpreter can grasp the most clearly defined action more quickly.
- A style letter sometimes ranks higher in its family than the areal alternative.
- It can be a more natural choice than a multi-areal letter.
- Style characters sometimes mesh well with the use of assumption.
- They add color to the language of Nactation; they're stylish!

It is easy to appreciate the above justifications for the use of style characters, especially if one has fully digested sections 8,10 , and 13 and/or is well practiced with Nactation.

Sections 1 and 2 cover the fundamentals of the most commonly utilized style characters: P (Point), \$ (Slot), H (Hit), X (hit and split), and K (Kill; hit twice).

The remainder of this section introduces the other four style letters: $\mathrm{T}=\mathrm{sTack} /$ Tower, $\mathrm{L}=$ Lift, $\mathrm{W}=$ Wild, and non-doublet $\mathrm{Q}=$ Quadruple split.

In position \#25 (below, left), Black has rolled 43. Having escaped a checker and leading in the race, he need not be embarrassed to play 43T, even though it merely shuttles a checker from one tall point onto another, as shown in 25.1 (below, right).


Similarly, if Black rolls 41 in \#25, he should bring one checker down from the midpoint, sTacking it with 41T, as shown in 25x (below, left). This move can also be nactated 41D.

Also shown in $25 x$ is 32 T (same move, but with a roll of 32 instead of 41 ). It is incorrect-or at best inadvisable-to nactate this move 32D, which (as clarified by the 6 pt convention in section 10) translates to the blotty move shown in 25 y (below, right).

stands for Lift, as in Lifting a blot to the safety of an occupied point.


In position \#26 (above, left), Black should hit (obviously) with his 4, and Lift his blot with the 2 , as shown in 26.1 (above, right). By playing $L$, he cannot be hit back.

T and L are most often used for moves that play a single checker. T and L are sometimes interchangeable, though a conscientious nactator will select the letter he believes his readers will most quickly grasp in the situation.

T (sTack or Tower) must add to a point that, when the move is completed, will contain four or more checkers. L can add to a point that ends up with three or more checkers.

L (Lift) moves a blot, whereas T can move a blot or spare, or even break a point.

For more explanation and examples of L and T , refer to \#69-71.

When using or interpreting style characters, think about what the terms mean in normal backgammon discussion. That approach will often serve you better than mechanically following rules and guidelines.
stands for Wild. It refers to a move that both splits and slots (i.e., "splots"). The checkers that move both end up as blots. Ain't that wild?


In position \#27 (above, left), Black has rolled 41. His split-and-slot move of W shown in 27.1 (above, right) is indisputably wild. However, it is also stronger than any other move available, including the reflexive choice (not diagrammed) of making the bar point!

The areal way to nactate the move in 27.1 is E. It resembles Black's E move in 15.1 (although there the ace happens to cover a blot instead of creating a new blot).

W is frequently interchangeable with E -or with C , if the near-side checker crosses the bar. However, E or C can be used even when one or both halves of the move cover a point, safety a blot, and/or float or spread a spare. By contrast, the narrowly defined but stylish W describes a very loose move, typically starting a point in both inner boards.

For more on W and the other slot-related families, see \#29-32 and \#72-73.
means Quadruple split. " Q " refers to a loose splitting move on the far side of the board that leaves the player with back checkers on four or more points.


Position \#28 is the opening position of the popular variant "Nackgammon" (for more info, go to http://www.nackbg.com/nackgammon.htm). One strong opening move is 62Q, the Quadruple split shown in 28.1. Other strong openers are 41Q, 52Q and 63Q.

The above definition of Q applies only to non-doublets. When applied to a roll of doublets, Q has a different meaning-see section 16 .

Congratulations: you now know how to nactate with 22 of the 26 letters of the alphabet!
In section 16, you can find definitions for the remaining four letters ( $\mathrm{F}, \mathrm{G}, \mathrm{M}$ and Y ) as well as clarified usage for other letters when doublets are rolled.
[Starting with section 7, traditional point numbers (1-24) are included in the text and around the diagrams. For example, " 11 " beneath the lower edge of a diagram labels Black's 11 point, abbreviated in the text as Black’s (or the) "11pt." White’s point numbers are mirrored on the opposite border.]

## Section 7: Symbols

A "symbol" is a character that is neither letter nor numeral. The current list is: $\$, \%, \&$, @, \#, ^, <, >. These symbols can be written, or they can be typed from a standard (U.S.) keyboard using the Shift key. (All but the last two are on the top row.)

\$stands for (single) Slot, introduced in section 1. You "slot" by playing a checker to a vacant forward point (7pt or lower). If doing so uses only part of the roll, the other portion of the roll must: be played down (to or within the outer board), or enter from the bar (or be forced). [This is the "down clause."]

\# 29 51S-41K-1-52V-21H-43H-63R-65H-31@-51T-51

In position \#29 (above), Black has 51 to play. The "down clause" written into \$’s definition is satisfied with $13 / 8$. There is a choice of points Black can slot with the ace, but as the 5pt trumps other points, the move shown in 29.1 (below, left) is $\$$.

By the same token, bringing down a 2 , 3 or 4 and slotting $6 / 5$ with the ace is nactated 21\$ (White's move in \#4), or 31\$, or 41\$ (White's move in \#12). On the other hand, $13 / 76 / 5$, which slots two points lower than the 8 pt, is not $61 \$$ but rather $61 \&$ or 61 N . (See the similar example in \#32.)

stands for alternate slot: a slotting move that is secondary, based on the three conventions listed above position \#72. For convenience, the $\%$ symbol is located just to the right of $\$$ on the keyboard.

The move shown in 29.2 (above, right) is delegated the secondary symbol \%. (" $51 \%$ " in the caption means 51 alt-slot, not 51 percent!) The 7pt takes a back seat to the 5pt. [For reference, the areal alternative for 29.1 is N (see section 4), and for 29.2 it is D.]

Position \#30 (below) is identical to \#29 (above), except that the checker on Black's 24pt has been moved back one pip to the bar.


In the variant position above, Black has the same 51, but this time he must enter from the bar with half the roll. The definition of $\$$ allows for this entrance; the solely remaining portion of the roll can now be slotted without a portion coming down.

Slotting the 5pt as in 30.1 is $\$$ (primary); slotting the 7 pt as in 30.2 is \% (secondary).


Note your alternatives of E, W or 5 for 30.1; and B, w or 7 for 30.2. (Refer to sections 4, 6 and 9.) For moves that enter-and this is true for most characters, not just for \$-you can choose to nactate either the remaining portion or the entire move.

For further discussion of \$ and related families, refer to section 13 (starting above \#72.)

## \& stands for double slot. By common usage, the ampersand represents the word "and." To relate this to Nactation, think "slot \& slot." Also, the ampersand is vaguely suggestive of two criss-crossing \$ signs.

The \& (double-slot) symbol refers to slotting two forward points, (i.e., below the 8pt). For preference of points slotted, see the which point convention above \#72.


In \#31, Black, who trails substantially in the race, rolls 32. The thematic move is \&, the double-slot move shown in 31.1 (below, left), which aims to quickly build a strong board. This move's most competitive candidates are likewise swashbuckling: W, shown in 31.2; and E, shown in 31.3. (Note that Black's move in 27.1 is both W and E.)


While it is natural to prefer the descriptiveness of \& and W, the areal alternative for 31.1 is A (for other examples, see 15.3, 16.3 and 53.5), and for 31.2 it is c (refer to 16.2). For lower-case letters, see section 10.

Further clarification: a move creating two new blots (on points lower than one's own 8pt) is regarded as a \& (double slot) move rather than a \$ (single Slot) move.

Do not confuse Black's 62\& move in \#32 (right) with his 62\$ move shown in 32x (below, right—a copy of position \#4).

For Black’s move in \#32 (large diagram), " 62 N " is a common areal alternative. The areal choice for the move in 32x (small diagram) is 62o; see section 10 .

White's opening 21\$ move (in both diagrams) also leaves two blots, but a checker higher than one's 7pt does not qualify as "slotted." Hence, the singleslot symbol (\$) is appropriate. The areal alternative is 21 N .

stands for anchor. (The symbol looks like a circled "a," the first letter of the word "anchor.") An anchor is a defensive point, usually in the opponent's inner board, sometimes in her outer board.

Grab a board and play through the sequence of moves (listed in the caption) that occurred to reach position \#33 below. On her last turn, White rolled 32; she entered from the roof with the 3 and covered that checker with a 2, thereby anchoring with 32@.


In \#33 (above), Black has rolled 65. His best move is to make a defensive point (anchor) with @ as shown in 33.1 (below, left). A reasonable alternative is to make an offensive point with $\mathbf{P}$, shown for reference in 33.2 (below, right).
 to the right of @ (the primary anchor symbol) on the keyboard.


In position \#34, Black has a choice of anchoring moves (either of which is better than hitting). He can make the 18pt anchor with @, as shown in 34.1 (below, left), or he can make the less advanced 20pt anchor with \#, as shown in 34.2 (below, right).

\$ and \% are the first two members of the Slot "family," while @ and \# are the first two members of the anchor "family." For further explanation, see sections 10 and 13.
[The \# sign that precedes each of the feature diagram numbers is merely a formatting element I chose for this tutorial. In context, it is easily distinguished from the \# (alt anchor) symbol that is written after the roll or is otherwise discussed in context.]
stands for fan (dance, stay off, fail to enter). The caret is suggestive of an upward arrow, pointing to the roof (the location of the fanning checker/s).
stands for enter one checker. If you like, you can think of < as meaning to enter less than (fewer than) 1.5 checkers.
stands for enter both/all checkers. If you like, you can think of > as meaning to enter more than 1.5 checkers.


In position \#35 (above), Black has two checkers on the bar. If he fans, you can list the roll plus $\wedge$. For example, the caption in $35 x$ (below, left) indicates that Black fanned with $31 \wedge$ (the only difference between \#35 and 35x being the player on roll).

If you have no reason to convey the specific roll that fanned (66, 63, 61, 33,31 or 11), you can replace $31 \wedge$ with "fan," "Fan," or simply "F," omitting the roll entirely.

If one of the checkers enters, you list the roll followed by <. In 35y (below, middle), Black entered one checker on White’s 2pt with $21<$. If you care about neither the exact roll nor the uniformity of using three characters (i.e., roll plus Nactation character) for every move, you can provide just the entering number, "2" (instead of " $21<$ ").

If Black enters both (or all four) checkers, you can list the roll followed by >. In $35 z$ (below, right), Black entered both checkers with 42>. Listing just the roll ("42") is also fine (unless, perhaps, if it's the final move of a sequence). When a move is forced, it is common to give only the roll, omitting the Nactation character completely.


Avoid using the enter both/all symbol when a player enters two (or three) checkers with doublets and two (or one) portions of the move remain. For example, in \#35, if Black rolls 22, then regardless of his move, the Nactation of > conveys incomplete information.

File names (for computers): When you save the rollout result of an early game position on a computer, its Nactation sequence typically makes a great file name.

The use of angle brackets <, >, is an exception. On most computers, angle brackets are used to redirect output and so cannot be part of file names. The easiest way around this (and it is a recommended textual option anyway) is to omit angle brackets and list just the two-number roll for a full entrance or a one-number roll for a single-checker entrance.

For more on file names, refer to the end of section 14.

## Section 8: Assumption

As Part 2 of this tutorial (i.e., section 10 and beyond) makes clear, Nactation, when properly used, is a precise language. When expert nactators or computer programs communicate with each other, there is no possibility of ambiguity.

On the other hand, nactating perfectly requires a non-trivial amount of study. With this in mind, I am wrapping up Part 1 of the tutorial with the art of "assumption." This shortcut technique endows you with a complete system, making it possible to handle any move that is likely to arise (even a tricky doublet) with a single character. The main prerequisite is that both nactator and interpreter employ a modicum of common sense.

Even if you are determined to become a concert nactator with complete exactitude in your selections, reading sections 8 and 9 will make it easier to interpret characters to which other people-those with incomplete Nactation skills-might resort.

In position \#36 (below, left), three aces are obvious: entering is forced, and Black should (of course) make his powerful 5pt. Assume, therefore, that the reader will know these three aces are played, reaching the position shown in 36x (below, right).


Oddly enough, Black would be better off stopping with the three aces played in 36x, but the rules of backgammon require him to play a fourth ace. Black's four plausible options, in descending order of strength, are shown in the small diagrams below.


Other Nactations are possible; for example, the Lifting/sTacking ace in 36.4 can sport T instead of L . The main point, though, is that by applying the art of assumption, it is unnecessary to apply the advanced concepts explained in later sections (that with areal precision identify the moves for $36.1,36.2,36.3$ and 36.4 as $\mathrm{E} ., \mathrm{E}, \underline{y}$ and $\underline{Y}$, respectively).

In position \#37 (below, left), Black has double 6s to play.
All reasonable candidate moves involve Black bringing down two checkers, as shown in the small diagram 37x (below, right). That part of the move can be assumed.


Black's move in 37.1 (below, left) is nactated Z -see the table of doublets in section 15. However, if Black comes Up with the third 6, there is only one good fourth 6 (coming down); therefore, $\mathbf{U}$ is fine. Indeed, even if the reader mentally plays Up with the 6 first, he'll quickly realize there is only one laudable way to play the other three 6 s .

For the moves in 37.2 and 37.3, you can similarly use assumption by keying off of 37 x if you like, though appraising four 6 s from \#37 yields the same letters. The move shown in 37.2 is $\mathbf{D}$ (coming Down), and the move shown in 37.3 is $\mathbf{P}$ (Pointing on the 1 pt ).


37.2 ...66D

37.3 ...66P

For \#37 and related positions, this ditty will help you remember the best move by score:
(1) At double match point, double Up. At gammon save, save Up;
(2) Get your money Down.
(3) At gammon go, to gammon is the Point.

It is common to assume a hit (or hits) for part of a roll. In most cases, you can nactate the leftover part of a hitting move without fear of someone misinterpreting you.


Position \#38 (above) is a valid example. "Clearly," Black should hit with two 4s, shown in the partial-move diagram 38x (above, right). We can nactate the other half of the move.

Black's best option is to run out with his other checker (covering the first one), as shown in 38.1 (below, left), nactated R. In truth, assumption is unnecessary for this move: running two checkers out with double 4 s is R even if there is no blot to hit.


A good alternative (and the best move at gammon go) is to bring the other two 4s Down, with $\mathbf{D}$, as shown in 38.2 (above, right).

The 38.2 move is properly nactated B , but the benefit of assumption is that you and your reader need not know the hit-more-6 rule (explained in section 10). As D is surely not meant strictly (13/9(4) in \#38 would leave a blot on the midpoint!), it is obvious that assumption has been applied. Hit, come Down, and then of course cover that checker.

The above example helps to demonstrate a useful axiom: the weaker the strict-usage move would be, the more confidently one can implement assumption with a given letter.

Even when hitting is not part of the best move, it often works to apply the hit assumption. After all, unless one is hitting, it is natural to play doublets in point-advancing pairsmoves that are covered by basic letters.

Logically, then, the assumption of a loose hit can be a convenient resource for describing a wider variety of candidate moves without the advanced doublets knowledge found in sections 15 and 16.

The four positions below each show a competitive move for Black at some match score with double 3 s in reply to White's opening 43D:


The above moves are nactated with four of the BEACON letters (from section 3). But Black has additional choices. Let's back up to the position before he made his move:


As a free-wheeling principle, you may "assume" that Black hits with three 3s as shown in 39x (above, right), allowing you to use a letter for just the final 3. In 39.5 (below, left), Black comes up with $\mathbf{U}$, and in 39.6 he comes down with $\mathbf{D}$. That seems sensible enough.


You must put yourself in the shoes of your readers, however-even if you are nactating moves to be replayed later by yourself. How are they going to interpret U or D in \#39?

The answer to this question hinges in part on the playing strength of your readers and the degree to which they flow with assumption. However, what is typically even more relevant is the strict-usage translation of the letter in the position at hand: how reasonable is that move compared to the move you intend to communicate?

Granted, the moves diagrammed above in 39.5 and 39.6 are merely third and fifth best, but I've seen experts play both. According to the \#39 rollouts (located in section 17), these moves are relative equity losses of only .028 and .033 (respectively) for money, and only .007 and .010 at double match point.

Technically, 33U means to make the opponent's bar point, and 33D to make one's own bar point, with relative evaluations of -.150 and -.230 : a whopper and a double-whopper compared to the moves diagrammed. The use of assumption seems reasonable here.

The non-assumptive areal letters for the moves shown in 39.5 and 39.6 , respectively, are R and S (see section 15). There is also a good non-assumptive style alternative for 39.6, which is H (noting the down clause mentioned in \#8 and above \#67).

Final observation: For 43D-33, 39.6 shows the best move that one can reasonably call D, because Black cannot hit in his own outer board. Compare with 63S-33 in \#59, where a vastly superior and legitimate D move (pointing on the bar point in 59.1) is available. There (in \#59), identifying 24/15* 13/10 (where only one of four portions is played in Black's outer board) as "D" would surely convey the wrong impression.

In conclusion, be careful not to assume too casually. It is worthwhile to consider (in a given position) what a letter might otherwise mean to make sure it is not misleading.

Examples of assumption continue in the next section.

## Section 9: Numerals

Instead of going with a letter (A, B, C...) or symbol (\$, \&, @...), you frequently have the option of nactating with a numeral ( $1,2,3 \ldots$ ). It is a convenience to which you can resort when you are not sure that you would be correctly communicating, or that your reader knows enough to correctly interpret, a letter or symbol for a given move.

A numeral simply represents the last digit of the traditional point number, and is the final destination for at least one of the checkers being played. For example, " 1 " means playing a checker to the $1 \mathrm{pt}, 11 \mathrm{pt}$ or 21 pt , and in that order of priority.

Numerals obey no strict rules, and should be interpreted assumptively: For example, "3" implies, "I'm playing a checker to the 3pt and you figure out the rest!" That said, for any remaining portions of the move that do not seem obvious, you may be aided by conventions (see section 10 and the summary at the end of section 13).

Suppose you know little Nactation beyond the first two or three sections of this tutorial. For \#40 (below), you merrily nactate the first six moves with basic letters, and then...


From \#40 (above), you need to nactate Black's move of $13 / 8$ 10/4. If you (or perhaps your readers) are fuzzy with definitions or conventions, you can use " 4 " to describe the $10 / 4$ portion of the move, very reasonably assuming your readers will see that $13 / 8$ surely accompanies it (as shown in 40.1, below left), as any other 5 is abhorrently worse.

Like reasoning can be applied to 40.2 and 40.3. Relative values of the three moves are unimportant. What matters is that if the 6 is played to the $4 \mathrm{pt}(4)$ or to the $2 \mathrm{pt}(2)$, then $13 / 8$ (in 40.1 or 40.3 ) is the obvious 5 ; or if the 5 hits on the 1 pt (1), then $13 / 7$ (in 40.2 ) is the obvious 6 . Any other choice with the leftover number leaves a double direct shot.


When implementing assumption (with a numeral or otherwise), nactate the less (or least) obvious portion of the move. For example, if you identify $13 / 8$ as " 8 ," granted the best 6 is then $10 / 4$ (shown in 40.1 ), but that 6 's edge over $13 / 7$ is small compared to the edge that $13 / 8$ has over $8 / 3$ or $6 / 1^{*}$ if $10 / 4$ (i.e., " 4 ") is put on the board first. In other words, nactate the hard part; you want the unstated part of the move to be as obvious as possible.

If you find it unsettling to rely on such assumptions, cultivate the (more robust) areal letters and familiarize yourself with the hierarchies explained in Part 2. For reference, the three moves above, respectively, are $\mathrm{o}, \mathrm{N}$ and $o$, with style options of $\$, \mathrm{H}$ and $\$$.

Flush with success after having numerically nactated the 40.1 move, you identify the next three moves of the game sequence easily (as $\mathrm{H}, \mathrm{H}$, and P ), before reaching this position:

\# 41 65R-65R-65R-43D-53D-52P-654-21H-42H-32P-63

In position \#41 (above), Black has a choice of two good moves. This example helps demonstrate the principle of giving priority to the lower point number.

There are two moves in the 4 family. The primary member 4 is shown in 41.1 (below, left), and the secondary member 4 (see section 14 for italics) is shown in 41.2. That is, the 4 pt is prioritized over the 14 pt . For reference, P (Point) or O (Outer) on the left, and $R$ (Run) on the right, are the orthodox characters.


Instead, suppose the roll in \#41 is 54 . In that case, as only part of the move (8/4) covers the 4pt, one must assume $13 / 8$ is the 5 . Hence "4," though reasonable, is a less bulletproof choice with 54 than with 63 . (For 23/14, you should certainly eschew a numeral, as all four legal moves that cover the 4 pt could, in theory, rank higher in the 4 family.)


With a roll of 33 here, the best move is to bring two checkers down, pointing on the 7pt, as shown in 42.1, which can be nactated 7. This is the same move made in 59.1 (White's builder differing by 1 irrelevant pip), nactated there with the standard D.

You might similarly choose 5 and 3 for the moves respectively shown in 42.2 and 42.3 (below). After playing a blot to the 5pt or 3pt, it is only logical to cover it; then for the other two 3s, hitting is "clear" and is a common assumption anyway.

If all three diagrammed moves are referenced together as 7,5 and 3 , there is a sense of consistency, just as there is if you label the three moves $\mathrm{D}, \mathrm{O}$ and N . (Instead, $\mathrm{P}, \mathrm{O}, \mathrm{N}$ is fine, though P conflicts with the areal theme.)


Lest you lose touch with basic characters or your assumptions become too lax, it is inadvisable to treat numerals as a major option. Sometimes, however, you encounter a position where numerals are a compelling fit, even when a non-doublet is rolled. To wit:


In \#43 (above), Black has a choice of three inside points he can make. Once you have digested the hit-more-6 rule (section 10) and italics (section 14), then for moves 43.1, 43.2 and 43.3, respectively, you can use P, $P$ and p; or you might prefer I, a and A.

Numerals are the alternative: 3 for the 3 pt, 4 for the 4 pt, and 5 for the $5 p t$. In most cases, I prefer letters (or symbols), but the simplicity and clarity of numerals in this case make them irresistible. There is no crisper way to distinguish these moves than 3, 4 and 5.


Unless you are fairly fluent in the use of complex doublet letters (see sections 15-16), numerals may be your best resource in some positions. For example...


In \#44 (above, left), Black would prefer to stop after making the 5pt in 44x but must legally play two more aces. His four best moves (in order of strength) are shown below. The respective areal Nactations of the four-ace moves are I, O., n and i (or the style letters P for the first, and p for the fourth, are available).

Numerals are a fine option. With the obvious 5pt made, 6 and 9 (shown in 44.1 and 44.3) are telegraphed. For 44.2, 0 (for 10pt) is clear enough; you don't specify the 10 pt if continuing to the 9 pt, and slotting the 7 pt volunteers a double shot, leaving only $6 / 5$ as the obvious fourth ace. Finally (bottom right), 4 puts a checker on the 4 pt , and of course it should be covered, again so as not to a leave a double shot.


From the reader's / interpreter's perspective, there are two ways to reason out characters that may have a built-in assumption. We'll use " 6 " (reaching 44.1) as an example.

- Assume the obvious 6/5(2) for two of the aces, as shown in 44x. Then, play a checker to the 6 pt as " 6 " suggests. (This was the method outlined.)
- Starting from \#44, imagine a checker played to the 6 pt (i.e., " 6 "). Then, with the other two aces, make the obvious 5pt. (This method is at least as common.)

Employing either mental procedure (neither of which seems clearly superior to the other) leads to diagram 44.1. It is helpful to be aware of both.

# Nactation <br> Tutorial <br> by Nack Ballard 

## Part 2

Advanced Nactation

## Section 10: Hit-more-6 Rule

You will sometimes encounter situations-even when non-doublets are rolled-that, given your knowledge so far, would be ambiguous. If the same letter is used for two different candidate moves, how can the reader guess which move is made?

Until now, U (also known as UV) is the only "family" that has been illustrated in this tutorial. If there are two legal up moves, you use U for one and V for the other (as explained beneath 20.2). How does one handle similar dualities for the other 24 letters?

Lower-case letters ( $\mathrm{a}, \mathrm{b}, \mathrm{c} . .$. ) to the rescue! The capital letter is the primary member of its family, and the lower-case letter is the secondary member.

To determine which of two moves of similar type earns the capital, there is a "hierarchy" of moves. Usage rules are designed such that the capital-letter move is stronger (i.e., a better backgammon move) than the lower-case-letter move most of the time.

Letter (and symbol) families conform to three important conventions, in the order of priority listed below. Collectively, these conventions are known as the hit-more-6 rule.

## Hit convention

Hit if possible, and on the higher point.
[Exception: An extra point in the home quadrant overrides any hit.]

## More points convention

Making or retaining more points has next preference. (The 24pt and 23pt do not count as owned points.)

## 6pt convention (order of priority)

1. Point owned: closer to the 6 pt (tie goes to the inside point).
2. Blot/spare destination: closer to 6pt trumps (except in one's own outer board, where farther from 6 pt trumps).

Above all (i.e., even over the hit-more-6 rule), one must honor each letter’s underlying definition. For example, P means to make a Point, and A has a specific areal imperative. In \#45 (below), therefore, 64P or 64A translates to 8/2 6/2 (whether it hits or not), never 24/20*/14*. Conventions operate only within the integrity of a letter's definition.

The hit-more-6 rule is fully spelled out above. Throughout this section, I will isolate elements of it, in order of priority, so that each can be clearly demonstrated.

Let us start with the Hit convention.

## Hit convention

Hit if possible, and on the higher point.
[Exception: An extra point in the home quadrant overrides any hit.]

Allow me to expand on the admittedly compact line that is highlighted above:

Priority is given to the move that hits as many times as possible. Given a choice of moves that hit the same number of checkers, prioritize the move that hits on the higher point.
(The "exception" underneath the highlighted line is dealt with in \#53.)

## R, r

" R " and " r " both refer to running back checker(s). I will now begin to integrate and clarify the roles of capital and lower case.


In \#45 (above), Black should of course hit two checkers, as shown in 45.1 (below, left): this move can be nactated $\mathbf{R}$ for Run (though more commonly K for Kill). On the other hand, if Black plays 24/18 with the 6 and then hits only one checker (perhaps oversight or timing finesse) as shown in 45.2 (below, right), it is nactated with a lower-case r.


In short, the hit convention prioritizes hitting as many checkers as possible. Accordingly, capital R (the head of its family) hits two checkers, and lower-case "r" hits one checker.


In \#46, Black can run in two different ways, either way hitting one checker. Hierarchy of $\mathrm{R} / \mathrm{r}$ is decided by the other part of the hit convention: hitting on the higher point. Thus, $24 / 20^{*} / 14$ (shown in 46.1 ) earns capital $R$, and $24 / 18^{*} 14$ (see 46.2 ) gets the lower-case $r$.



## K, k

"K" stands for "Kill," which means to hit twice. The secondary member of the K family is the lower-case "k."

Another approach in \#46, though inferior to (hit and) Run, is to Kill, with the second hit being on the 2 pt . As with the R family, the main hit on the 20 pt earns the capital letter (K, see 46.3, above left) and the hit on the 18pt gets the lower-case letter ( $k$, see 46.4).

## U, V

U stands for Up (to play up), and V stands for Variant up. However, U and V have the same underlying definition: to play back checker(s) to or within the area from the 24 pt to the 18pt.

U and V are the only letters that share a family. U is the primary and V is the secondary member of the U (or UV ) family, just as R is the primary and $r$ is the secondary member of the R family. ( U is introduced in \#7, and V is compared to U in \#18-20.)


Black's move shown in 47.1 (below, left) is $\mathbf{U}$, simply because it hits. The move in 47.2 (below, right) is the lower-ranked $\mathbf{V}$ because it does not hit.


What happens when (within a letter's definition)... it is not possible to hit? or... when two moves hit the same number of checkers? or... when two moves hit on the same point? In any of these cases, we use the next highest priority determinant (isolated below):

## More points convention

Making or retaining more points has next preference. (The 24pt and 23pt do not count as owned points.)


In variant position \#48 (above), there is no White blot for Black to hit. Assignments are therefore based on the more points convention. The move shown in 48.1 is $\mathbf{U}$, and the move shown in 48.2 is $\mathbf{V}$, because the former (the one on the left) makes an extra point.

[As you will realize when you learn part 2 of the 6pt convention: without the existence of the more points convention, the above U and V designations would be reversed.]

For reference, the symbol @ (anchor, see \#33) is a correct (and more common) alternative for the move shown in 47.2 and 48.1.

## P, p

 "P" (primary) and "p" (secondary) both refer to making a Point. The letter $P$ is introduced in \#3 and expanded upon in \#63-66.

Position \#49 (above) illustrates a subtler example of the more points convention. Black's two best moves in the P family (which also happen to be best overall) hit on the same point; we therefore count the number of points owned after each move is made.

Covering the 3pt as in 49.1 (below, left) is capital $\mathbf{P}$ because it gives Black a fifth point on the board. (Never count the 24pt.) Making the 5pt in 49.2, which merely trades the 7 pt for the 5pt, ends up with one fewer point (four) and therefore gets the lower-case $\mathbf{p}$.

[The only other member of the $P$ family from \#49 is $6 / 4 / 3$ without hitting (ugh). Moves with 24/22 are not in the $P$ family, because part of the roll is left over. Refer to \#63.]

What happens when two moves have the same hitting status and end up with the same number of points? In that case, we move another rung down the ladder: we break the tie by implementing part 1 of the 6 pt convention:

## 6pt convention (order of priority)

1. Point owned: closer to the 6 pt (tie goes to the inside point).
2. Blot/spare destination: closer to 6 pt trumps

> (except in one's own outer board, where farther from 6pt trumps).


For position \#50 (above), making the 7pt as shown in 50.1 (below, left) is nactated $\mathbf{P}$. Making the 4 pt as shown in 50.2 (below, right) is assigned the lower-case p. The 7pt earns the capital letter because it is closer (than the 4 pt is) to the 6 pt .


Note that when owned points are equidistant from the 6pt, tie goes to the inside point. That is, 5 pt beats 7 pt , 4pt beats 8 pt , 3pt beats 9 pt , 2pt beats 10 pt , and 1 pt beats 11 pt .

In review of 49.1 and 49.2, the 5 pt is closest to the 6 pt , but two points (3pt +7 pt ) beat one ( 5 pt ). By contrast, moves 50.1 and 50.2 end up with the same number of points. The 6 pt convention is considered only when the resulting number of points is equal.

## More points convention

Making or retaining more points has next preference.
(The 24pt and 23pt do not count as owned points.)

## 6pt convention

1. Point owned: closer to the 6 pt (tie goes to the inside point).
2...

Before moving on, take note of the parenthetical directive highlighted above. It relates both to the more points convention (above it) and part 1 of the 6 pt convention (below it, just discussed). Even if the 24 pt or 23pt contains two or more checkers, it does not count as an owned point. (A second checker on either point is classified as a "spare.")

For understanding the reasons behind the 24pt-23pt directive, and for learning the other part of the 6pt convention, opening 53 of Nackgammon (below) is a good case study.

## S, s

S is a basic letter that stands for "Split" (large number up, small number down). It is introduced way back in \#5. Capital " $S$ " is the head of its family; lower-case " $s$ " is the secondary member.

## Z, z

Z, a companion letter for the above, stands for "reverse split" (small number up, large number down). For details, see \#6. Capital " $Z$ " is the head of its family; lower-case " $z$ " is secondary.


We will examine four families of moves (in order of strength, except for $S$ ).

There are two ways to come up with the 3 and down with the 5 . Even with two or more checkers on it, neither the 24 pt nor 23 pt is counted as a point; therefore, part 2 of the 6 pt convention, highlighted in the text box below, determines $\mathrm{Z} / \mathrm{z}$ ranking.

The destination of the 20 pt is closer (than the 21 pt is) to the (one's own) 6 pt ; thus the move shown in 51.1 (below, left) is $\mathbf{Z}$, and the move shown in 51.2 (below, middle) is $\mathbf{z}$.

## 6pt convention (order of priority)

1. Point owned: closer to the 6pt (tie goes to the inside point).
2. Blot/spare destination: closer to 6 pt trumps
(except in one's own outer board, where farther from 6pt trumps).


While S and Z are different families, a convenience clause (introduced in \#6) permits the use of $S$ when it is not legally possible to play up (i.e., split) with the larger number. Such is the case with opening 52, 53 and 54 in backgammon, but not in Nackgammon. For reference, see 51.3 (above, right): S comes up with the larger number (the 5).

Next is the U family. There is only one way to come up with the 5 , which means, as before, that the way the 3 is played determines U/V ranking. Again, the 20pt is closer (than the 21pt is) to the 6pt; hence, the move shown in 51.4 is $\mathbf{U}$ and 51.5 is $\mathbf{V}$.


A popular alternative for the move in 51.5 is Q . Interestingly, the same position is reached in 28.1 (nactated U or Q ) with a different roll of the dice.

Finally, let's look at the R family. Once more we apply part 2 of the 6 pt convention. Running to the 15 pt as shown in 51.6 (below, left) is capital $\mathbf{R}$, and running to the 16 pt in 51.7 is dealt the lower-case $\mathbf{r}$. The 15 pt is a pip closer (than the 16 pt is) to the 6 pt .


In \#51, if Black's opening roll is 54, 63 or 62 (instead of 53), similar reasoning applies: the move that runs out farther (closer to the 6pt) earns the upper-case R, and the move that runs less far gets the lower-case r. If, however, Black's roll is $65,64,61,52$ or 43 and he chooses to run, there is only one R-family move and the 6 pt convention is irrelevant.

The unifying theme of the $\mathrm{Z} / \mathrm{z}, \mathrm{U} / \mathrm{V}$ and $\mathrm{R} / \mathrm{r}$ pairs above is that the higher-ranked move is determined by part 2 of the 6pt convention (closest blot). If the 23pt were counted as a point (which it isn't), part 1 (closest owned point) of the 6 pt convention would determine the capital, and both $\mathrm{Z} / \mathrm{z}$ and $\mathrm{R} / \mathrm{r}$ would be reversed (with owned 23pt trumping 24pt).

It is no coincidence that (for \#51) $\mathrm{Z}, \mathrm{V}$ and R are stronger moves then their respective counterparts ( $\mathrm{z}, \mathrm{U}$ and r ). In the early game, there is little difference in value between the owned 23pt and owned 23pt, and split back checkers are often worth more than either. With this knowledge, Nactation ignores whether the 24pt or 23pt is made.


Position \#52 (above) closely resembles position \#46. If Black hits on the 20pt and then, instead of running with the 6 (as in 46.1), he comes down with the 6 -he has made a move in the Z (reverse split) family. As with \#51, both legal Z moves have the same status for hitting, for the more points convention, and for part 1 of the 6 pt convention.

## 6pt convention (order of priority)

1. Point owned: closer to the 6pt (tie goes to the inside point).
2. Blot/spare destination: closer to 6pt trumps (except in one's own outer board, where farther from 6pt trumps).

When the difference in blot/spare status is in one's own outer board, farther ranks higher (as indicated by the yellow-highlighted phrase above). The destination of the 9pt in 52.1, being farther from the 6pt (than the 7pt is in 52.2), ranks higher and earns the capital $\mathbb{Z}$.


We solve the S family (Split: big number on far side, small number down) the same way. The destination of the 11 pt , which is farther (than the 9 pt is) from the 6 pt , ranks higher; therefore, S is $24 / 18^{*} 15 / 11$ (see 52.3, below left) and s is $24 / 18^{*} 13 / 9$ (see 52.4).


I'll restate (though less eloquently) part 2 of the 6pt convention: Prioritize blot/spare destination in this point-by-point order: 6pt, 5pt, 4pt, 3pt, 2pt, 1pt, 12pt, 11pt, 10pt, 9pt, 8pt, 7pt, 13pt, 14pt, 15pt... 24pt. In short: 6pt $\rightarrow$ 1pt, 12pt $\rightarrow 7 \mathrm{pt}$, 13pt $\rightarrow$ 24pt.

The reversal of the blot/spare destination paradigm in the outer board is sometimes called the "wrinkle." The wrinkle exists for two important reasons:

- Moving from behind the midpoint (e.g., from the 15pt) typically rescues a blot. That blot naturally lands farther from the 6pt than does a midpoint spare.
- A blot closer to the 6pt (e.g., on the 7pt: vs 9pt, 10pt or 11pt) is more exposed.

For concrete examples, compare 52.1 to 52.2, and 52.3 to 52.4 (above). For both pairs, the left-hand move (with the capital letter) is greatly superior to the right-hand move.

The hit-more-6 rule is designed for areal letters, though P and @ conform. It also works in large part for the remaining style families $\mathrm{H}, \mathrm{X}, \mathrm{K}, \mathrm{T}, \mathrm{L}, \$$, \& and W (see section 13, including the "summary of conventions" at the end). The hit-more-6 rule should not be applied to numerals, except perhaps as a guideline (see section 9, paragraph 3).

For additional reinforcement, the entire hit-more-6 rule is repeated below:

## Hit convention

Hit if possible, and on the higher point.
[Exception: An extra point in the home quadrant overrides any hit.]
More points convention
Making or retaining more points has next preference.
(The 24pt and 23pt do not count as owned points.)

## 6pt convention (order of priority)

1. Point owned: closer to the 6 pt (tie goes to the inside point).
2. Blot/spare destination: closer to 6pt trumps (except in one's own outer board, where farther from 6pt trumps).

You may find it easier to combine the more points convention with part 1 of the 6 pt convention. This gives you at most three bite-sized concepts to check:

- Hits: quantity and quality
- Points: quantity and quality
- Blot/spare destination: distance from 6pt


## Section 11: Hit-more-6—Supplement

The previous section covers the overwhelming majority of hit-more-6 situations you are likely to encounter. In the interest of completeness, however, I provide this section to cover offbeat cases. In truth, it is only the first of these, the home quadrant exception, to which you should pay any real attention.

Home quadrant exception: This is an important corollary to the hit-more-6 rule: "An extra point in the home quadrant overrides any hit." Without it, terrible moves that break (or fail to cover) an inside point-in order to hit-would often be awarded a capital letter, and stronger, structural candidate moves would be lower-ranked within their families.

\# 53


From position \#53 above, we examine a few of the ways Black can play his roll of 42. For each pair below, the vastly superior move appears in the left-hand diagram, helping to demonstrate that an extra point in the home quadrant is typically worth more than a hit.




The scenarios subsequently presented are increasingly rare. Unless you are a theoretician, programmer or puzzle aficionado, you may prefer to skip the rest of this section. On the other hand, if you enjoy detailed clarity or esoterica, feel free to dive in!


Lower quadrant dictates: In position \#54 above, Black has 64 to play. Consider 54.1 versus 54.2. By 6 pt convention, the 14 pt (closer to the 6 pt ) trumps the 15 pt -note that intermediate/temporary destinations do count. On the other hand, the 11pt (farther from the 6 pt) trumps the 10 pt. How is this apparent ( 6 pt convention) conflict resolved?

The lower quadrant is given priority. Here, the near-side outer board is lower (has lower point numbers) than the far-side outer board. Therefore, 21/15/11 (in 54.1) is awarded the capital S, and 21/14/10 (in 54.2) gets the lower-case s. The 11pt beats the 10pt.

As the 9 pt is less far (from the 6 pt ) than the 10 pt and 11 pt , the plays shown in 54.3 and 54.4 are third and fourth in the $S$ family (italic $S$ and $s$ ): The order of these two moves is determined by the secondary destination: the 14 pt is closer (to the 6 pt ) than the 15 pt .


The lower-quadrant-dictates directive helps to clarify the prioritization of blot/spare destination: $6 \mathrm{pt} \rightarrow 1 \mathrm{pt}, 12 \mathrm{pt} \rightarrow 7 \mathrm{pt}, 13 \mathrm{pt} \rightarrow 24 \mathrm{pt}$. (See also the last page of section 10 .)

The sole member of the Z family is shown in 54.5 (far right). Note that the move in 54.2 is not in the Z family—you do not move the 4 before the 6 with 20/16/10—because of the high-number-first directive explained on the next page.

High number first: To prevent (non-doublet) areal letters from functionally overlapping (and rather to preserve more capitals), the following directive applies: When a single checker makes the entire move (without hitting mid-journey), the higher of the two numbers rolled is played first for purposes of determining that move's family.

\# 55 63S-62X-63H-64H-55S-64H-63R-43K-11E-51 or -42

In \#55 above, Black should play 13/9. Obeying the high-number-first directive, the 5 is played before the 1 , and the 4 before the 2 . Thus, with either 51 or 42 , the move shown in 55.1 is D and not in the Z family. (Without this prudent rule, $15 / 9$ would be in both families and the move in 55.4 would be demoted to third place in its ranking, italic $Z$.)

Likewise, if Black opts for $9 / 3$, 51 is played $9 / 4 / 3$ and 42 is played 9/5/3 (higher number first), not $9 / 8 / 3$ and $9 / 7 / 3$. That is, $9 / 3$ (see 55.2) is in the A family and not the $O$ family.

55.1 ...51D or 42D

55.2 ...51A or 42a

This paragraph is a reminder that the more points convention trumps the 6pt convention. From position \#55, with a roll of 42 , moves in the Z family anchor with the 2 and come down with the 4 . The move covering a fifth point (55.3, below left) earns the capital $\mathbf{Z}$.


For additional clarity, below is a contrived variant of \#55. (Black's checkers are on the same points.) In position \#56, Black's 15/9 move is no longer in the D family because he cannot play $15 / 10$ or $15 / 11$ first. (Here, 51 D is $13 / 89 / 8$, and 51 d or 42 D is $13 / 7$ !)


Here, the only way to play $15 / 9$ with 51 is $15 / 14 / 9$, nactated Z—or optionally S by convenience clause (defined above \#62).

In a similar vein, the only way to execute $15 / 9$ with 42 is $15 / 13 / 9$, nactated z or s . (Capital Z or S is reserved for $24 / 22$ 13/9, which makes an extra point.)

Likewise, because of White's anchor blockade, Black's $9 / 3$ is no longer in the A family, and instead $9 / 8 / 3$ or $9 / 7 / 3$ is O . (Here, $51 \mathrm{~A}=8 / 3 / 2$, and $42 \mathrm{~A}=8 / 6 / 2$ !)
[For style letters such as P , "high number first" is irrelevant. In both positions with 51, or in \#56 with $42, \mathrm{P}=9 / 3$ and $\mathrm{p}=15 / 9$. Note, however, in \#55 with 42 , the vacant 4 pt makes the ranking $\mathrm{P}=8 / 46 / 4, \mathrm{p}=9 / 3$, and (third member) $P=15 / 9$. To verify these rankings, review the 6pt convention, part 1, including "(tie goes to the inside point)".]

The high-number-first directive is relevant only if all three of these conditions apply:
(1) One checker makes the entire move without hitting mid-journey, and
(2) The high number is not initially blocked (as it is in \#56), and either
(3) (a) the high number can pass the 13pt or 7 pt but the low number cannot, or (b) the second number played (high or low) passes the 13pt.

Please do not bother committing the above criteria to memory! I list it only to instill a sense of how infrequently the high-number-first directive actually matters.

High number from high point: Once in a blue moon, you'll encounter a situation (with a non-doublet) whereby two moves in the same family keep/make the same points and yield identical checker destinations! In such a case, final tie-break priority is given to the higher of the two numbers originating from the higher point (i.e., from farther back).


In \#57 (above), Black can play up with the 3 and cover with the 2 , or he can play up with the 2 and cover with the 3 . The points owned and blot/spare destinations of both moves are the same. In this rare scenario, the capital $\mathbf{E}$ is awarded to 57.1 (below, left)—which plays the higher number (the 3 ) from the back, and the lower-case $\mathbf{e}$ is assigned to 57.2.


Logic Loop: The hit-more-6 rule contains an obscure logic loop that in theory creates a conflict in the way that some moves are ranked within a family.


For \#58 (above), the two highest-ranked moves in the E family (not diagrammed) each move a back checker, cover the 3pt, and end up owning six or seven points on the board.

The conflict arises when we compare low-ranked moves to each other. The move in 58.1 adds an extra point to the home board, thereby overriding the hitting move in 58.2; that move in turn overrides 58.3 (which keeps the same two inside points without hitting). Yet 58.3 (which makes a sixth point) beats 58.1 by the more points convention!


Something has to give. The rule patch is: If and only if a logic loop arises, the move with the extra home board point (58.1, in this case) outranks the other two.

In practice, it is extremely improbable you'll ever see a logic loop position, let alone that someone will make one of the (terrible) loop moves. The three moves above, ranked $4^{\text {th }}$, $5^{\text {th }}$ and $7^{\text {th }}$ in the E family, are strength-wise ranked $8^{\text {th }}$ (whopper), $15^{\text {th }}$ and $16^{\text {th }}$ (triple whoppers). It is a safe bet that you'll never have to nactate such a move from a real game.

## Section 12: Definitions-Movements

The early sections of this tutorial supply simplified definitions, so that it as easy as possible to understand and use Nactation on the first two or three moves of the game.

Broader functions of letters have been gradually incorporated into this tutorial, but not all high-level usages have yet been elucidated. Clarified definitions are provided in this section (for areal letters) and in the next section (for style letters).

## Down

In traditional terminology, "down" refers to playing from the far outer board to the (near) outer board. In Nactation (except for non-doublet S and Z), down portions may optionally be played within (i.e., both from and to) the near outer board.


With Black's 33 here, two D-family moves obey the "hit" and "more points" conventions. The 6 pt convention breaks the tie. The owned 7 pt is closer (than the 10 pt is) to the 6 pt ; therefore, the move in 59.1 (below, left) is awarded $\mathbf{D}$, and the move in 59.2 is $\mathbf{d}$.


Here, two (in 59.1) or one (in 59.2) of Black’s 3s are played from 10pt to 7pt: within the outer board. Such a movement is common for a down portion. Similarly, in \#59, with 21D, 41D, 51D and 61D (respectively), 13/11 8/7*, 13/9 8/7*, 13/8/7*, and 13/7* 8/7 contain two down portions (one from the midpoint and the other from the 8 pt ).

Down portions are handled the same way for other areal letters (e.g., N and O ), and for any style characters that are affected (e.g., H and \$). It is only non-doublet B, S and Z that have a restricted down portion, whereby either the near outer board or the far outer board is disallowed as a possible source quadrant (see \#62).

## Far-side Portions

Back checker movements (with the exception of the carefully partitioned R and U , which we'll get to) apply to the entire far side - not just to the rearmost quadrant.


In sections 1-4, the far-side portions for all the illustrated moves were confined to the back quadrant. It is now time to expand our horizon to include the far outer board; to that end, position \#60 (above) provides a useful backdrop.

With a roll of 52, Black should play $18 / 13$ with his 5 , which is as legitimate a far-side portion as any other far-side 5 (e.g., Bar/20 or 23/18 or 21/16 or 20/15) would be.

If the deuce is played within the outer board (most conservative but best), the move is $\mathbf{B}$ (shown in 60.1). If the 2 Crosses from outer to inner board, the move is $\mathbf{C}$ (60.2). If the 2 is played inside, the move is $\mathbf{E}$ (60.3). Note how similar these moves look to those shown in $17 \mathrm{x}, 16.2$ and 15.1, once you perceive the far side as a single area of movement.


By the same token, a portion played in the far outer board can be the far-side part of an $S$ (or Z ) move. For convenience, the S diagram appears directly beneath the B diagram. The difference is that for B , the down portion is played within the outer board, whereas for $S$ it is played into the outer board. (This difference will be reviewed shortly, in \#62.)
[For purposes of assigning the right family, the move shown in 60.4 should be regarded as $S=18 / 13 / 11$, not $Z=18 / 16 / 11$. (Refer to \#55 for the high-number-first directive.)]

Diagram 60.5 is included only for reference. You might well have nactated this move (24/22 18/13) correctly a long time ago—after reading halfway through section 1.

The entire-far-side concept also pertains to the multi-areal families (Q, F, G, M and Y; see section 16). Applicable style families (e.g., W, X and @) fit the criteria as well.

## Running

To "Run" means to advance one or more checkers on the far side, with at least one portion of the move played to or within the area from the 17pt to 13pt. (Many examples can be referenced: \#3, 38.1, 45.1, 46.1, 51.6, 60.5, 74.1 and 89.1 —plus 61.1 below.)

The next position helps to demonstrate the distinction between R and U .


Consider \#61 (above). The five best moves (below), all made on the far side, are ranked by hierarchy (determined by the 6pt convention) within each family.


Recap: For moves played purely on the far side (with apologies to Gary Larson for yet another apparent reference to one of his cartoons), those that have at least one destination in the $17 \mathrm{pt}-13 \mathrm{pt}$ area are in the R family. Those that do not are in the U family.

In Nactation, there is no such thing as "running" past the midpoint. Review position \#54 for clarification: there, R can only be 21/15 20/16 (not diagrammed), whereas 21/11 (shown in 54.1) and $20 / 10$ (shown in 54.2 ) are in the S (split-and-down) family. Likewise, 60.4 is not an R move; the sole R-family option for \#60 is shown in 60.5 .

## Splitting

In Nactation, "S" is short for "Split," which in turn is short for "Split-and-down." It refers to a (non-doublet) move that satisfies the two aspects below. It plays both
(1) the larger number on the far side, and
(2) the smaller number from the far outer board to the near outer board.

The first aspect includes the possibility of breaking an anchor (which is the traditional definition of split) but is actually very liberal: it refers to any far-side checker movement.

The second aspect is not the standard down portion (playing to or within the outer board), but rather a restricted down portion: the checker is played from the far outer board.
"Z" stands for "reverse split." Its definition mirrors that of S above (under 1 and 2)— with the words "smaller" and "larger" transposed.

Convenience clause: When it is impossible to play the large number on the far side or the small number down to the near side, S may be used in lieu of Z. (See \#6 and \#56.)

## Division of Labor for B, S and Z

B, S and Z are closely related letters that work in harmony to ensure that capital letters can be used a high percentage of the time.

Non-doublet division of labor: B, S and Z are all composed of a far-side portion and a restricted down portion. For S and Z , the checker must come from the far outer board (as outlined a few paragraphs back). For B, the checker must come from the near outer board-the source and destination are both in the 12pt-7pt area.

For examples of B, S and Z non-doublet usage, see \#5, \#6, \#17 \#51-52, \#54-56 and \#60. The additional example below directly compares all three families.


In position \#62, Black rolls 42. We will contemplate three moves.

If Black enters with the 4 (the far-side portion) and covers the 9 pt with the 2 (within the outer board), he has played $\mathbf{B}$, as shown in 62.1 (below, left). If he enters with the large number (the 4) and plays the small number (the 2 ) down from the midpoint, the move is S, as shown in 62.2 (middle). Finally, if he enters with the small number and brings the large number down, the move is $\mathbf{Z}$, as shown in 62.3 (right).


In \#62, what about bar/219/7 and bar/23 11/7? Those moves are in the B family because the front checker moves (with either the large or small number) within the outer board. In failing to cover a point (compare to 62.1), these horrendous moves (not diagrammed) are relegated to lower-case b and italic $B$ (see section 14), respectively.

Doublet division of labor: For doublets, B, S and Z all play the front checker(s) "down" in the unrestricted (standard Nactation) sense; i.e., to or within the outer board.

For doublets, B has the highest profile of the three letters, but S and Z each handle a slice of B's responsibility. B refers to two "runs" (far-side portions) and two "downs" (down portions); S refers to three runs and one down; and Z refers to one run and three downs. For examples of B, S and Z applied to complex doublets, refer to \#77 and \#83.

To view a helpful BSZ crosstable for both non-doublets and doublets, refer to this post: http://www.bgonline.org/forums/webbbs_config.pl?noframes;read=150096

## Run, Down, Jump and Inside

Most of this section has been devoted to explaining and qualifying the Run and Down portions of moves. It is worth a reminder that, while they may require less explanation, Jump and Inside portions are an integral part of Nactation's areal design.
"Jump" (introduced in \#21) means to Jump over the bar-to play a portion (or portions) from the outer board to the inner board. "Inside" (introduced in \#23) means to play inside-to play a portion (or portions) entirely within the inner board. [I modify the traditional definition of the "inner board" to include the 0pt (the bear-off tray).]

In the quest to thoroughly understand Run, Down, Jump and Inside portions and the areal letters they affect, the material at the end of section 5 and beginning of section 15 (with graphic illustrations in both places) is worth reviewing more than once.

## Complex Doublets

Complex doublets are moves for which checkers are not played in simple pairs. If you dislike assumption, or if you aspire to nactate even the trickiest moves for a literal reader or computer in a way that is totally free of ambiguity, sections 15 and 16 are for you!

There are 35 ways to combine the four categories of checker movements-run, down, jump and inside. For two-category moves, BEACON letters (along with doublet S and Z) are used. R and U handle moves where all portions are on the far side. D, J and I take care of near-side possibilities. Q, F, G, M and Y cover the rest. Again, see sections 15-16.

Learning complex doublets is the most challenging part of Nactation, but keep in mind:

- Complex doublets represent only a small percentage of moves made.
- You can nactate without such advanced knowledge (unless interfacing with a computer). Virtually all moves, even those with complex doublets, can be adequately communicated by judicious use of "assumption" (see sections 8-9).


## Section 13: Definitions-Style Characters

The previous section clarifies the definitions of movements, which mainly affect areal letters. This section clarifies the definitions of style characters.

## P, pm@,\#

"P" (Point) is introduced in section 1 (\#3), and @ (anchor) in section 7 (\#33). However, an important prerequisite, called the "dedication clause," is that the entire move is used to make (or cover) a single point. Entering or forced portions of a move are waived.

For position \#63 or \#64 below, Black can cover his 10pt with the 3 . However, there is an ace left over. Therefore, the P family cannot be properly used for any move that includes $13 / 10$. The P (or @) family is reserved for moves that are dedicated to making a point.


This pair of diagrams affords you the opportunity to practice using the hit-more-6 rule. In each of the two positions, can you identify the moves that are fully dedicated to making a point and determine their rankings within the P or @ family?

In position \#63 (above, left), a hit trumps no hit. $\mathbf{P}$ refers to making the 7 pt while hitting-known as "pointing on" the 7pt, and p refers to making the 5pt (without hitting). The resulting moves of 63.1 and 63.2 are diagrammed in the left-hand column below.

In position \#64 (above, right), Black must settle for making a point without hitting. The 7 pt and 5 pt are equidistant from the 6 pt , but as part 1 of the 6 pt convention states (see the clause highlighted above \#50), tie goes to the inside point. Therefore, $\mathbf{P}$ refers to making the 5 pt in 64.1 , and p refers to making the 7 pt in 64.2 -see the right-hand column below.



For covering the 20 pt in 63.3 and 64.3 you can use italic $\boldsymbol{P}$, and for making the 21 pt in 63.4 and 64.4 you can use italic $\boldsymbol{p}$ (the third and fourth members of the $P$ family; see \#76).

However, there is no prize for showing off. If, instead of $P$ and $p$, you wisely select the Nactation symbols of @ (anchor) for 63.3 and 64.3, and \# (alt-anchor) for 63.4 and 64.4, you spare both yourself and your reader from having to first find, count and/or compare the point-making possibilities on the near side. (See also \#33.)

Primary members of an areal family often communicate more clearly than non-primary members of a style family. For example, instead of p, you can use A for 63.2, and D for 64.2. (You can similarly replace the primary members—D for 63.1 and A for 64.1 -but with less purpose.) Even more cogently (putting aside @ and \# for a moment): for 63.3 and 64.3 , U is easier to grasp than $P$; and for 63.4 and $64.4, \mathrm{~V}$ is easier to grasp than $p$.


Position \#65 (above) spotlights a subtlety. Covering the 5pt requires just three deuces; however, playing "through" the existing 11pt checker with $13 / 5$ (shown in 65.1 , the top left diagram of the four below) does qualify as a dedicated Point-making move. Conversely, a move that combines $11 / 5$ with a 2 other than $13 / 11$ is not in the $P$ family.



All four P-family candidates legally playable from \#65 are shown above. The 65.4 move is ranked last by the more points convention: it fails to add a new point. The other three plays are ranked by ownership of a point closest to the 6pt (part 1 of the 6pt convention); they make the 5pt, 9pt and 2pt, respectively. (For italics, see section 14.)

The moves shown in 65.2, 65.3 and 65.4 -which admittedly are horrendous alternatives to 65.1-have areal Nactations of D, I and A, respectively.


In position \#66 (above), Black enters with one deuce. This entering portion of the move is waived (an allowance that is included in the definition paragraph above \#64). With the remainder of the move, we consider only portion(s) that conspire to make or cover a single point. It happens that two such moves are very close in value.

The 9/7/5*/3 move in 66.1 (below, left) earns the capital $P$ because it hits. (Even if it did not hit, the owned 3pt is closer to the 6pt than the owned 20pt is for the p move in 66.2.)


The move in 66.3 dedicatingly makes the 4pt (playing "through" the 6pt qualifies). Even so, it is outranked by 66.2 because, in giving up the $8 p t$, it ends up with three points instead of four. (Remember, the 24pt does not count.) Refer to section 14 for italics.

## H, h

"H" (introduced in section 2) means to Hit loose, and also to hit only once. If, in doing so, there is a single leftover portion of the roll (not counting entering or forced portions, which are waived), it must be played down (to or within the outer board). This is the "down clause."

I'll clarify by referencing a few moves. H can be used for 13/10*/9 in \#1 or for 13/11*/10 in \#70 (where the continuation to a vacant point is an accompanying down portion that honors the down clause); or for 89.1 (by waiving the entering portion). However, H may not be used for 63.1 and 69.1, where the checker that hits fails to stay loose.

Given that (in part) H and X are defined as hitting exactly once, and K is defined by hitting exactly twice, the number of hits does not figure into their familial rankings. We can therefore strip away all but the final nine words of the italicized paragraph above \#45 (the clarifying expansion of the "hit convention"), and rephrase to:

Hit on the higher-numbered point (i.e., to gain more pips).
For simplicity's sake, this "higher point" subset convention can and should be used in lieu of the entire hit convention for $\mathrm{H}, \mathrm{X}$ and K .

After honoring the underlying definition of $\mathrm{H}, \mathrm{X}$ or K and the above sub-convention, any tie is broken by the more points convention, followed by the 6 pt convention. In other words, the rule for H is "higher-more-6" (instead of hit-more-6).


In position \#67 above, Black has 62 to play. Hitting on the (higher) 14pt as shown in 67.1 (immediately below, left) is H. Hitting on the (lower) 7pt and using the "down clause" for the non-hitting portion of the move as shown in 67.2 (right) is $\mathbf{h}$.

"X" means hit and split. Unlike $H$, there is no down clause. (An X move splits instead.) In 67.3 and 67.4 (above), Black hits with the 6 and "splits" (see section 12) with the $2 . \mathrm{X}$ (anchoring in 67.3) obeys the more points convention, thereby trumping $x$ (in 67.4).

To avoid functional overlap, X never hits on the far side (see \#8). Do not, for example, claim that 67.1 is also an X move because Black splits with 22/20 then hits with 20/14*.

The four moves above earn the same Nactations (H, h, X, x) with a roll of 22 as with 62. However, take great care using style letters for doublets. If, after obeying the underlying definition and any explicitly stated convention, there is still a leftover portion, a style letter is technically improper-in that case one is invoking assumption (see section 8).

## K, k

K (introduced in 8.1) stands for Kill, which means to hit exactly twice (with no leftover portion, unless it enters or is forced).


In \#68, after Black hits from the bar with the 5 , he has a close choice of which second checker to hit. Because the 18pt is higher than the 4 pt , the move shown in 68.1 (below, left) is $\mathbf{K}$, and the move in 68.2 is $\mathbf{k}$. This hierarchy for a roll of 54 applies likewise to 52 .


## L, l

"L" is introduced in \#26. It means to Lift a blot to an owned point (thereby increasing the number of checkers on it to at least three).

Particular to L and T , an extra convention is inserted into the hit-more-6 rule, in this way: Hit-more-fewer-6. The "fewer" stands for fewer blots.


To qualify a move for the L family, it is permissible (from \#69, above) to create a blot with part of the move (13/9*) in order to Lift it (9/8) as shown in 69.1 (L, below, left).

The move that lifts the 23pt blot, shown in 69.2 (below, middle), is the secondary member of the L family (l), only because 69.1 hits. If 69.1 did not hit, then instead 69.2 would be primary because it is the only move that leaves zero blots.


The 69.3 candidate (right), which can be nactated R or T , also qualifies as a Lifting move because its $14 / 13$ portion lifts a (created) blot. Granted, 69.3 is reprehensible: it is outranked by 69.1 using any one of the four conventions in the hit-more-fewer-6 rule!

\# 70

In position \#70 (above), Black, with his roll of 21, has a few different ways he can safety the blot on the 9pt. One way is to use the blot as a builder to make the 7pt. However, he has two superior moves, both of which include Lifting his blot to the 8 pt with the ace.

It comes down to how the deuce is played. Hit-and-Lift (see 70.1, below left), which honors the hit convention, earns the capital L. Anchor-and-Lift (see 70.2), which honors the more points convention (and fewer blots convention), gets the lower-case ranking (l).


Lifting the blot to the 6pt, shown in 70.3 (right), obeys the low-priority 6pt convention, but its only real "virtue" is that it leaves fewer blots than 70.1. This pathetic move, which neither hits nor makes a point, is firmly demoted to third place in the L family.

Strictly speaking, the T family is off limits for the moves in 70.1 and 70.2 . [It can be used with assumption (see section 8) if you believe your reader will interpret T and t as you intend!] The only actual T move is shown in 70.3. Refer to the upcoming segment.

Areal Nactations for the above three moves are d, B and O, respectively.
"T" (sTack or Tower) was introduced in \#25. Explained for the first time here, the definition of T includes a form of the dedication clause: all checkers played must end up on points that (when the move is complete) will contain four or more checkers. Entering (or forced) portions are waived.

Apply the same set of conventions to T that you do to L: Hit-more-fewer-6.

Usually, T is a simple, straightforward move that sTacks one checker onto a single point (for example, 13/8 in diagram 25x). For the position shown below, some of the resulting T-family moves stack two checkers onto a point, or stack checkers onto two points.


In \#71 (above), Black's best four moves, all of which sTack, appear-in order of both backgammon strength and T-family ranking-on the next page.

None of the moves shown below hit or end up with more points than any of the others. The hit and more points conventions are thus irrelevant, and we move on to the third criterion of the hit-more-fewer-6 rule: fewer blots. In that regard, the two plays in the top row, which safety the 10pt blot, rank higher than the two plays in the bottom row.

To compare within each row, we finally check the second part of the 6 pt convention (blot/spare destination), and as Black's 2 is played the same way within each pair, we actually need to examine only how he plays his 5 . The 8 pt destination outranks the 13pt destination; therefore, in each row, the play on the left outranks the play on the right.

Putting together the previous two paragraphs makes it easy to determine rankings for the four plays, which can be seen in the captions: T, t, $T$ and $t$. (For italics, see section 14.)


Areal Nactations for the above four moves are D, B, O and C, respectively,

Why is it that T has a dedication clause included in its underlying definition, while L does not? There are two reasons:
(1) This difference decreases the functional similarity of L and T . For example, if L had a dedication clause, then both these style letters (instead of just T ) would be unusable for moves like 70.1 and 70.2.
(2) If T had no dedication clause, its value would be diluted by move portions that strip one point and over-stack another. For example, for \#25, (capital) 32 T would be $24 / 218 / 6$ instead of the much stronger $13 / 8$ move shown in $25 x$; the hitch is that T is largely destination-oriented, and by 6pt convention the 6pt beats the 8pt. By contrast, L focuses more on the source (a blot in need of being safetied); its lack of a dedication convention does not incur a dilution of such magnitude.
" $\$$ " (previously described in sections 1 and 7), is the primary member of the Slot family; "\%" is the secondary member.

Definition of \$: Playing a checker to a vacant forward point (7pt or lower). If there is then one leftover portion of the roll (not counting entering or forced portions, which are waived), it must be played down (to or within the outer board). ["Down clause."]

The slot families (\$, \&, W) apply chiefly to non-doublets. They may be used properly for doublets when two or three portions are forced (e.g., bar/23(2) 13/11 6/4), or loosely with assumption (see sections 8 and 9 ). Generally, though, to precisely nactate a doublets move (one that slots or otherwise), avoid style letters and refer to sections 3, 15 and 16 .

The Nactation of slotting moves boils down to three conventions, in this order of priority:

## Slotting Priority

(1) More points convention: make or keep the most points.
(2) Which point slotted: 5pt, 4pt, 7pt, 3pt, 2pt, 1pt (order of preference).
(3) $6 p t$ convention. (See section 10.)


In \#72 above, Black has 32. To honor the down clause of \$’s underlying definition, Black slots with one number and comes down with the other. By "which point," the 5pt outranks the 4 p ; thus, $\$$ is as depicted in 72.1 (below, left) and $\%$ is as depicted in 72.2.


In \#73 above, Black again has a roll of 32. This time it is possible to cover an extra point (the 10pt), thereby honoring "more points." In this case, therefore, slotting the 4 pt is $\$$ as shown in 73.1, and slotting the (otherwise preferred) 5 pt is $\%$ as shown in 73.2.


With the 3 slotted $8 / 5$, either of two deuces honors the down clause. By the 6pt convention (final tie-break), in the outer board the 11pt is farther (than the 8 pt is) from the 6 pt , and therefore $13 / 11$ (see $\%$ in 73.2 ) ranks higher than $10 / 8$ (see italic $\$$ in 73.3 ).

Instead of the \$ family for the above five moves, you can use the N family (for some) or O family (for others). For definitions of areal letters, see sections 4 and 5 . For selecting the proper member of a family, see sections 10 (upper/lower case) and 14 (italics, etc.).

Because hitting and slotting generally fail to support each other tactically, the families of \$, \& and W disregard the hit convention. By definition, a "slot" goes to a vacant point and therefore cannot hit; and if there is a non-slotting portion of the move, the fact that it might hit is incidental and irrelevant to the familial ranking.
[At one point in the evolution of Nactation, there were six slotting rules (one of which related to unstacking tall points). The extra rules further helped the best move to earn the capital letter, but they confused people. It is substantially easier to implement today's set of three conventions (listed above position \#72).]

## Summary of Conventions

The hit-more-6 rule (explained in section 10) applies in pure form to all areal letters, and to style characters P and @. Highest priority is a "hit" (overridden only by an extra inside point), next is "more" points; then break ties by " 6 pt." The two parts of the 6 pt convention are not difficult to understand but should be carefully reviewed.

To accommodate the specialties of style characters, the main conventions (hit, more points, 6pt) selectively cooperate with other conventions:

Because they already hit, $\mathrm{H}, \mathrm{X}$ and K are modified to higher-more-6. (Above \#67.) L and T have a "fewer blots convention" inserted: hit-more-fewer-6. (See \#69-71.)

For \$, \& and W, use: more-which-6 (see conventions listed above \#72). For \& and W, mainly focus on "which point"-as more points and 6pt seldom come into play.

The underlying definitions of H (see \#67) and \$ (see \#72) include the "down clause." The definitions of P, @ (see \#63-66) and T (see \#71) include the "dedication clause." The latter is also implied for H and $\$$ as long as the down clause is taken into account.

Assumption: To nactate loosely, using few or no conventions, see sections 8 and 9.

## Section 14: Italics (and other hierarchy)

In Nactation, each letter has its own family, for which upper case (capital) is primary and lower case is secondary. (Many examples are illustrated in sections 10-13.)

Occasionally, you might want to resort to the third (tertiary) and fourth (quaternary) members of a letter family. For these, you use italics.

Examples of italics that have already appeared in this tutorial are $4, S, R, P, L, T$ and $\$$. (They caption various after-diagrams under \#41, 54, 61, 63-66, 69-71 and 73.)

## R, r, R, r

"R" (Run), which was discussed in \#3, \#45-46, \#51, and \#60-61, is defined precisely here: The destination of at least one portion is in the $17 \mathrm{pt}-13 \mathrm{pt}$ area; remaining destinations are entirely (and anywhere) on the far side.

\# 74 63R-21H-63U-41K-51-54K-31-53-51K-5-61U-21H-42@-63

In position \#74 (above), there are exactly four R-family moves (shown below). As there is no action on the near side (it remains unchanged), I diagrammed only the far side of the board for each move. Isolating the far side simplifies the comparisons.


For the set of four plays shown above, the 6pt convention is applied. It is the destinations of the 13pt, 14pt, 15pt and 16pt that determine the familial rankings of R, r, $R$ and $r$.

In \#74, the fifth and sixth best moves (not shown) are: $U=24 / 21$ 24/18, and $S=20 / 11$. To verify these moves are not in the R family, review the definition above position \#74.

$$
\mathrm{U}, \mathrm{~V}, \mathrm{u}, \mathrm{v}, \mathrm{U}, \mathrm{~V}, u, \mathrm{v}
$$

You will seldom encounter a situation with more than two strong moves for a family, but it is a less rare event with UV. Positions with extra recycled checkers may generate many back-quadrant moves that are not easy to describe with other letters. Hence the double-sized family. Lower case buys you four members, and italics eight members.


Position \#75 (above) occurs on the fifth roll of a Nackgammon opening. Black's best eight moves all play Up. Again, I've isolated the far side of the board for each diagram.

The 6pt convention-for points, then blots/spares-determines ranking in this example. (The 23pt is not an owned point; two checkers there are classified as spares.)


In live play, positions with more than four competitive moves within the same family practically never arise. Indeed, in the example above, there is only one: The U move in 75.1 towers in value above the other seven.

Notwithstanding, to demonstrate the depth of Nactation, I'll provide an example (below) of an eight-member situation in which the common basis is a family other than UV.

## P, p, P, p, P, p, P, p

" P " (for Point) is introduced in section 1 and expounded upon in \#49-50 and \#63-66. Keep in mind the "dedication clause," as it applies to P (and to @): the entire move (except for portions that enter from the bar or are forced) is used to make a single point.


As illustrated, both in the large-font P-letter sequence above and in the series of moves (76.1-76.8) captioned below, the fifth, sixth, seventh and eighth family members are written the same as the first four except they are emboldened (i.e., in bold font).

To determine hierarchy in a family, use the hit-more-6 rule. For example, 76.2 outranks 76.3 because the former hits and the latter does not. Making the 7/4 move without the hit as in 76.4 ranks below 76.3 because the (owned) 4 pt is trumped by the 7 pt .

In a real game, of course, only the first two moves ( P and p ) are worth considering; and, as a practical matter, you have no need to nactate moves that people never make!

Even if you did need or desire to nactate the other six moves, it would be unnecessary to resort to such low-ranked members. Instead, for example, you could use D, A, @, \# and v (respectively) for $76.3,76.4,76.5,76.6$ and 76.7 , and numeral 0 for 76.8.

76.7 ...21P

76.8 ...21p

Most of the time, emboldening can be safely used for emphasizing or spotlighting moves in a Nactation sequence. However, if a highly atypical move does arise-one that needs to be emboldened due to its low ranking in a family, you should find some other way to distinguish the moves you want emphasized (e.g., by highlighting or adding an asterisk).

Beyond that, changing color can in theory generate an infinite number of members; e.g.,


In this tutorial, for visibililty, I embolden letters in diagram captions (and tables). I have suspended that formatting convention for this entire section to eliminate confusion, especially so that the characters captioning 76.5-76.8 can be distinguished from those in 76.1-76.4. For good measure (given that color is discussed here), I've also suspended the blue typeface formatting that I use in the rest of the tutorial (except for \#58).

In short, Nactation hierarchy is: Upper/lower case, italics, bold, and (unlimited) colors. Again, though, you will seldom require italics, let alone the subsequent levels.

Symbols and numerals: Lower case does not exist for non-letter characters. For the slot family (\$, \%) and anchor family (@, \#), there is a second symbol in lieu of lower case. For other symbols, and for numerals, the family sizes are essentially cut in half: italics is the secondary ranking (and boldface is third/fourth, and colors are fifth-plus).

Some symbols can be clearly distinguished from their italic counterparts only when handwritten. While \$ \% \$ \% and \& \& are passable hierarchies, italic @ \# (when typed) too closely resembles non-italic @ \# (see?). Conversely, numerals italicize and embolden distinctively (e.g., 8888 ), but the assumptive application can cause uncertain rankings.

In truth, it is a reach to use a member ranked below secondary for symbols and numerals. Satisfactory alternatives are always available in any case.

File names (for computers): The standard for use of Nactation in naming files is relaxed. Aside from typing the correct dice rolls and choosing characters that aren't entirely misleading, you basically just need to avoid creating identical file names.

The only real conundrum you might encounter is that most operating systems do not distinguish upper- and lower-case letters. (Moreover, you cannot italicize, embolden, color or underline.) For example-though such pairs rarely arise-32Z-41H-11 and 32Z-41h-11 are different positions but you'll be prompted to overwrite. One way to resolve the conflict in this example is to change H to A , or h to I (or preferably both). Another way, perhaps easier but less elegant, is to name the second file 32Z-41hh-11.

For more on file names, refer to the end of section 7.

## Section 15: Doublets Table-BEACON

If you are adept with implementing and interpreting assumption (see sections 8-9), you can manage well enough without this section and the next. On the other hand, complex doublets are the most interesting to nactate, and if you you prefer to extinguish any possible ambiguity in your Nactation, you will find these sections useful (if not vital).

As outlined at the end of section 5, a doublets move is composed of four "portions." Each portion performs one of four basic checker movements (which can be used as nouns).



To or within the outer board


In each diagram above, the yellow highlight identifies all possible points from which a Black checker might originate (for a given move portion), and the checkers identify all possible Black destinations (for that same move portion). The captions further elucidate.

Every doublets move is a combination of four movements. There might be three "downs" and one "jump." Or two runs, one down and one inside. These are just two examples.

It should be clarified that "Run" has two definitions:

Run A move played entirely on the far side of the board, for which the destination of at least one checker is lower than the 18 pt -i.e., to the $17 \mathrm{pt}, 16 \mathrm{pt}$, $15 \mathrm{pt}, 14 \mathrm{pt}$ or 13 pt . [To review the distinction between Run and Up, see \#3 vs. \#7, \#51, \#61, and \#74-75.]

Run Any portion of a move played on the far side of the board. [This definition, introduced at the end of section 5 , is the one primarily used in this section and the next.]

All 35 possible permutations of four-portion moves are represented in the table below. The half on the right is a continuation; the gray " Q " row is the $19^{\text {th }}$ of 35 rows.

## Table of Doublets

| Letter | Run | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{B}$ | 2 | 2 |  |  |
| $\mathbf{S}$ | 3 | 1 |  |  |
| Z | 1 | 3 |  |  |
| E | 2 |  |  | 2 |
| E | 3 |  |  | 1 |
| E. | 1 |  |  | 3 |
| $\mathbf{A}$ |  |  | 2 | 2 |
| $\mathbf{A}$ |  |  | 3 | 1 |
| $\mathbf{A}$. |  |  | 1 | 3 |
| $\mathbf{C}$ | 2 |  | 2 |  |
| $\mathbf{C}$ | 3 |  | 1 |  |
| $\mathbf{C}$. | 1 |  | 3 |  |
| $\mathbf{O}$ |  | 2 | 2 |  |
| $\mathbf{O}$ |  | 3 | 1 |  |
| $\mathbf{O}$. |  | 1 | 3 |  |
| $\mathbf{N}$ |  | 2 |  | 2 |
| $\mathbf{N}$ |  | 3 |  | 1 |
| $\mathbf{N}$. |  | 1 |  | 3 |


| Letter | RUn | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Q}$ | 1 | 1 | 1 | 1 |
| $\mathbf{R}^{*}$ | 4 |  |  |  |
| $\mathbf{D}$ |  | 4 |  |  |
| J |  |  | 4 |  |
| I |  |  |  | 4 |


| $\mathbf{R}^{*}$ | 2 | 0 | 1 | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{D} \mathbf{D}$ | 0 | 2 | 1 | 1 |
| $\mathbf{J}$ | 0 | 1 | 2 | 1 |
| $\mathbf{l}$ | 0 | 1 | 1 | 2 |
| $\mathbf{F}$ | 2 | 1 | 0 | 1 |
| $\mathbf{G}$ | 1 | 2 | 0 | 1 |
| $\mathbf{M}$ | 1 | 0 | 2 | 1 |
| $\mathbf{Y}$ | 1 | 0 | 1 | 2 |
| $\mathbf{F}$ | 2 | 1 | 1 | 0 |
| $\mathbf{G}$ | 1 | 2 | 1 | 0 |
| $\mathbf{M}$ | 1 | 1 | 2 | 0 |
| $\mathbf{Y}$ | 1 | 1 | 0 | 2 |

* R row: If all portions are played to the 18pt or higher, use the U family (it's a subset).
* $\underline{\mathrm{R}}$ row: If both far-side portions are played to the 18 pt or higher, use the $\underline{\mathrm{U}}$ family.

The cell-filled colors of the rows (yellow, blue, gray, orange, pink, green) serve merely to distinguish parts of the table and similar letter groupings. The yellow-highlighted numbers on the right help to identify patterns. An empty cell implies a zero.

The easiest and most fun way to learn the doublets table is not to memorize it, but rather to understand the logic and absorb it through practice. With illustrated examples, I will explain the doublets table in three pieces, starting with the left half.

In the left half of the above table, find $B, E, A, C, O$ and $N$ (no underline, no dot) in the first row of each trio (22--, 2--2, --22, etc.). Elementary (simple doublet) examples of BEACON appear in positions \#9-14. Refined (complex doublet) examples appear below.


The upper row of each diagram set (above and below this paragraph) has three positions. In each position, Black is to play the letter in parentheses. Test yourself, if you like. The lower row shows each of the positions after Black has played the indicated letter.

A 2:2 ratio is applied in all positions. That is, for each of two selected areas (run, down, jump, inside), two (of four) doublet portions are played-and in one of three ways:

1. Simple pair: two checkers on a point move together, one portion each (e.g., 6/5(2)).
2. Two checkers from different points move one portion each (e.g., 24/22, 23/21).
3. One checker moves both portions (e.g., 13/10/7).

All possible ways to combine the move halves $(1+1,1+2,1+3,2+2,2+3$ and $3+3)$ are represented in diagrams 77.1 through 82.1. The elementary case of $1+1$ (simple pair for both halves of the move) is represented in 81.1-as it is in positions \#9 through \#14.


To grasp the basic idea, compare the move in \#9 to the move made in 77.1 and observe the conceptual similarities. Likewise, compare \#10 to 78.1, \#11 to 79.1, and so on.

To determine (or verify) a capital letter, apply the hit-more-6 rule (refer to section 10). For example, in \#77, Black’s two fours played "down" (to or within the outer board) prioritize hitting with 11/7* over making point(s); hence B = bar/21 24/20 13/9 11/7*. (Indeed, even b = bar/21 20/16 13/9 11/7* outranks $B=$ bar/21 24/20 13/9(2).)

So far in this section, we have examined only doublet moves for which two portions are played in each of two areas, covered by the letters in BEACON. For example, B (as seen in \#9 and 77.1.) is composed of 2 runs, 2 downs, 0 jumps and 0 insides. This combination can be abbreviated "22--" (or "2200") as it appears in the first row of the doublets table, the top three rows of which have been isolated below (left).

| Letter | Run | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{B}$ | 2 | 2 |  |  |
| $\mathbf{S}$ | 3 | 1 |  |  |
| $\mathbf{Z}$ | 1 | 3 |  |  |

If (instead of two runs and two downs), three runs and one down are played (represented by " $31-$-" in the table), the proper letter is S . If there are one run and three downs (13--), the appropriate letter is Z . Examples follow.


In \#83 (above), Black rolls 22. How do we nactate his four best moves (83.1-83.4)?

The moves shown in the top two diagrams (of the four-diagram set below) are in the S family by virtue of having three runs and one down. The moves in the bottom two diagrams are in the Z family by virtue of having one run and three downs. In this set, the more points convention (see section 10) determines the ranking within each family.


As noted, the correct usage of $\mathrm{B}, \mathrm{S}$ and Z for doublets differs from that of non-doublets. However, it helps to remember that in both cases, S plays more pips (i.e., the majority of the pips rolled) on the far side, whereas Z plays more pips in the outer board.

For usage consistent with the five B-related trios (E, A, C, O, N) in the first half of the doublets table, it is permissible to use $\underline{B}$ (underlined) for 31-- and B . (dotted) for 13--. However, the more elegant replacement letters of S and Z (respectively for $\underline{B}$ and $B$.) do have the excellent mnemonic support explained in the previous paragraph.

Next, let us examine the E, A, C, O and N trios, appearing beneath the $\mathrm{B}(\mathrm{SZ})$ trio in the first half of the table, which is reproduced below.

| Letter | Run | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{B}$ | 2 | 2 |  |  |
| $\mathbf{S}$ | 3 | 1 |  |  |
| Z | 1 | 3 |  |  |
| $\mathbf{E}$ | 2 |  |  | 2 |
| E | 3 |  |  | 1 |
| E. | 1 |  |  | 3 |
| $\mathbf{A}$ |  |  | 2 | 2 |
| $\mathbf{A}$ |  |  | 3 | 1 |
| $\mathbf{A}$. |  |  | 1 | 3 |
| $\mathbf{C}$ | 2 |  | 2 |  |
| $\mathbf{C}$ | 3 |  | 1 |  |
| $\mathbf{C}$. | 1 |  | 3 |  |
| $\mathbf{O}$ |  | 2 | 2 |  |
| $\mathbf{O}$ |  | 3 | 1 |  |
| $\mathbf{O}$. |  | 1 | 3 |  |
| $\mathbf{N}$ |  | 2 |  | 2 |
| $\mathbf{N}$ |  | 3 |  | 1 |
| $\mathbf{N}$. |  | 1 |  | 3 |

The plain letters (B, E, A, C, O, N) cover all situations in which two portions are played in one "area" (run, down, jump or inside) plus two in another area. (Review Section 3.)

The idea behind the underlined and dotted variants is straightforward. They cover all possible situations with three portions played in one area and one in another area.

For such moves (i.e., with a $3: 1$ or 1:3 ratio):

- When three portions are played in the higher-point area, underline the letter.
- When one portion is played in the higher-point area, add a dot (period).
"Higher-point" relates to the highest point from which checkers might originate. In that respect, areas are ranked from left to right in the table: run, down, jump, inside.

A diagram is worth a thousand words.


In position \#84 (above), Black has a roll of 33. His best moves are diagrammed below. In each case, three 3 s are played with a particular movement-run (in 84.1), down (in 84.2), or jump (in 84.3)—and the fourth 3 is played inside (6/3), in the lowest area.

The function of the underlined ( $\underline{B}$ ) EACON letters is similar to that of the plain letters used in 77.1 to 82.1 (and in section 3). The difference is that they apply to a $3: 1$ ratio (instead of 2:2): the letters captioned below- $\underline{\mathbf{E}}, \underline{\mathbf{N}}$ and $\underline{\mathbf{A}}$-are underlined accordingly.


In the "mini-table" below, I've extracted every third row of the main table (and changed the order to match the order of the diagrams). To reinforce your understanding, compare the $\underline{E}, \underline{\mathbf{N}}$ and $\underline{\mathbf{A}}$ moves made above (noting the $3: 1$ ratios) to the $\underline{E}, \underline{N}$ and $\underline{A}$ rows below.

For example, following the main position $\# 84 \rightarrow 84.1$, Black played $\underline{E}$, which consists of three "runs" (24/21 21/18 21/18) and one "inside" (6/3). In the corresponding $\underline{E}$ row of the mini-table, there is a 3 (three) in the Run column and a 1 (one) in the Inside column. (The move has no downs and no jumps: those cells are blank.)

| Letter | Run | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| $\underline{\underline{E}}$ | 3 |  |  | 1 |
| $\underline{\mathbf{N}}$ |  | 3 |  | 1 |
| $\underline{\mathbf{A}}$ |  |  | 3 | 1 |
| $\underline{\mathbf{C}}$ | 3 |  | 1 |  |
| $\underline{\mathbf{O}}$ |  | 3 | 1 |  |
| $\mathbf{S}$ | 3 | 1 |  |  |

To show that all 3:1 ratio possibilities have been covered, I have included the row for S (which is preferred as a substitution for $\underline{B}$ ).

An example of S appears earlier, in 83.1. From \#83 $\rightarrow$ 83.1, Black played three runs (24/22 24/22 23/21) and one down (13/11).


In \#85, Black's roll is 44 . His best moves are diagrammed below. You can (and should) verify that these $\underline{\mathbf{C}}$ and $\underline{\mathbf{O}}$ moves correctly correspond to the run/down/jump/inside representations in the $\underline{\mathrm{C}}$ and $\underline{\mathrm{O}}$ rows of the mini-table (posted above \#85).



Positions \#84 and \#85 generated (best) moves with 3:1 ratios. The next two positions (\#86 and \#87) will generate 1:3 ratios: moves for which one portion is played in a higher area of the board and three portions are played in a lower area of the board.


In position \#86 above, Black has a roll of 11. His best moves are shown below. In each case, one ace is played with a particular movement-run (in 86.1), down (in 86.2) or jump (in 86.3)—and the other three aces are played inside ( $6 / 54 / 3^{*} 4 / 3$ ).

The function of the (B.)E.A.C.O.N. letters is similar to that of the plain letters (\#9-14 and 77.1-82.1) and underlined letters (83.1-85.2), but with a $\mathbf{1 : 3}$ (instead of 2:2 or 3:1) ratio. The letters below are accordingly "dotted" (i.e, each one has a dot/period after it).


For practice, please verify that the E., N. and A. moves shown above correspond to the run/down/jump/inside allocations in the E., N. and A. rows of the mini-table below.

| Letter | Run | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| E. | 1 |  |  | 3 |
| N. |  | 1 |  | 3 |
| A. |  |  | 1 | 3 |
| C. | 1 |  | 3 |  |
| O. |  | 1 | 3 |  |
| Z | 1 | 3 |  |  |

To show that all 1:3 ratio possibilities have been covered, the Z row is included ( Z being the preferred substitution for dotted B.).

An example of Z appears earlier, in 83.3. From \#83 $\rightarrow$ 83.3, Black played one run (23/21) and three downs (13/11 11/9 11/9).


In \#87, Black’s roll is 22. His best moves are diagrammed below. You can (and should) verify that these $\mathbf{C}$. and $\mathbf{O}$. moves correctly correspond to the run/down/jump/inside allocations in the C . and O . rows of the mini-table (posted above \#87).


Technically, a dotted letter (such as E.) is two characters, though a dot (period) is forgivably small. That said, purists may prefer the single-character alternative of: E

The dot underneath the E is called a "combined ring below." To create it, I place my cursor after the E, then in Microsoft Word (2007), I navigate as follows: Insert / Symbol / More symbols / Symbols / Combining Diacritical Marks. There, in the bottom middle box I type the character code 0325 and click on Insert. Whew!

If you use the OÇE̊ÅN letters regularly, you can save time by leaving the Combining Diacritical Marks window open, or by storing those five characters somewhere (e.g., in a macro or at the bottom of your current document) and copy/paste as needed.

The copy/paste idea is even more practicable if your medium is html. Store this string: <span style="font-family: Arial Unicode MS, Helvetica, sans-serif;">E\&\#x0325;</span> Replacing the E in turn with A, C, O and N creates the other four strings.

Vertical spacing is an issue. When a diacritical mark is used in text, the line above is pushed upwards, and the line below downwards. To fix this in Microsoft Word (2007), position the cursor within (or highlight any part of) the paragraph. Open the Paragraph formatting dialog box, under the Index and Spacing tab set Line Spacing to Exactly, and to its right select a height (" 16 pt " in my case) that achieves the desired reduction.

| Letter | Run | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{E}$ | 1 |  |  | 3 |
| $\mathbf{N}$ |  | 1 |  | 3 |
| $\mathbf{A}$ |  |  | 1 | 3 |
| $\mathbf{C}$ | 1 |  | 3 |  |
| $\mathbf{O}$ |  | 1 | 3 |  |
| $\mathbf{Z}$ | 1 | 3 |  |  |

In the left column of the table above \#87, replacing E.N.A.C.O. with E̊NÅACOO causes those five rows to swell to twice their height.

I reduced the inflated E̊NACOO rows (so that they match the height of the Z row) by using the method described previously (Paragraph / Indents and Spacing / Line Spacing / Exactly).

Overall, I find the single-character version (with "combined ring below") more aesthetic as a reader, and as a writer I've gotten comfortable with it. However, I expect most people will adopt the more user-friendly after-dot. I am happy seeing either.

If your Nactation is handwritten, spacing is no problem, nor is there additional work: you simply jot the dot underneath (instead of to the right of) your OCEAN letter, giving you the visually preferred placement. Regard this "underdot" (designating the 1:3 ratio) as a contracted version of the underline (which designates the 3:1 ratio).

## Section 16: Doublets Table—R and F groups

The previous section covers the various BEACON families. This section finishes the doublets table with the " $R$ " and " $F$ " groups.


Let us first dispense with Q, which is in a row by itself (see the next mini-table below). Q stands for "Quarters," as one quarter of the move is played in each area.

In \#88 (above), Black rolls 33 . For his best moves (diagrammed below), he plays one 3 in each area (run $=21 / 18$ or $24 / 21$, down $=13 / 10$, jump $=8 / 5^{*}$, inside $=6 / 3$ ). By the $6 p t$ convention: the (owned) 18 pt earns the capital $\mathbf{Q}$, and the 21 pt gets the lower-case $\mathbf{q}$.

88.1 ...33Q

88.2 ...33q

For purposes of defining one of the four main areas, "run" applies to any movement on the far side of the board, including the back-quadrant portion of $21 / 18$ or $24 / 21$ shown above. The letter $U$ (up) distinguishes itself only as a non-doublets family (e.g., see \#75), and as a refinement to the R and $\underline{\mathrm{R}}$ rows of the doublets table (see \#89-90, upcoming).

## Uni-areal Doublets (4:0 ratios)

Next, let's consider the 4:0 ratio moves. (Relevant rows are colored in orange.)

Conveniently, the column and row headers of the table both supply the letters: R (or U), D, J and I.

Use one of these families when all four portions of a doublet share the same type of movement. For example if a move has four Downs, use D.

| Letter | RUn | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Q}$ | 1 | 1 | 1 | 1 |
| $\mathbf{R}^{*}$ | 4 |  |  |  |
| $\mathbf{D}$ |  | 4 |  |  |
| $\mathbf{J}$ |  |  | 4 |  |
| $\mathbf{I}$ |  |  |  | 4 |

*If all destinations are the 18 pt or higher, use U .

Here is a doublet position that further clarifies which of the R or U family to use:


In \#89 (above), Black rolled 22. His best moves play all four portions on the far side.

In 89.1 (below, left), where one or more of Black's destinations (the 14 pt ) is on a point numbered lower than the 18pt, the move is nactated $\mathbf{R}$. In 89.2 and 89.3, where no destination is lower than the 18pt, the moves are nactated with the $\mathbf{U}$ family (also known as the UV family), which can be reviewed at \#18-20, \#47-48 and \#75.


The three R- and U-family moves above exemplify 4:0 ratios. Each move is composed of 4 RUns and 0 (zero) other movements—no Downs, Jumps nor Insides.

Similarly, D, J and I each describe moves with all four portions played in its area. You can find such examples for D in diagrams 37.2 and 59.1 , for J in 22.1, and for I in 24.1.

## Tri-areal Doublets (2:1:1 ratios)

The remaining doublet possibilities are all 2:1:1 ratios. They are represented in the final twelve rows of the main table, reproduced in the subtable on the right.

Commit to memory the letter sequences RDJI and (the alphabetic) FGMY:

Picture yourself on a hot day in Yosemite National Park, looking down at a cool, refreshing lake. It makes you want to

## Run Down, Jump Inside

These words match the column headers of

| Letter | RUn | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{R}^{*}$ | 2 | 0 | 1 | 1 |
| $\mathbf{\underline { \mathbf { D } }}$ | 0 | 2 | 1 | 1 |
| $\mathbf{J}$ | 0 | 1 | 2 | 1 |
| $\mathbf{I}$ | 0 | 1 | 1 | 2 |
| $\mathbf{F}$ | 2 | 1 | 0 | 1 |
| $\mathbf{G}$ | 1 | 2 | 0 | 1 |
| $\mathbf{M}$ | 1 | 0 | 2 | 1 |
| $\mathbf{Y}$ | 1 | 0 | 1 | 2 |
| $\mathbf{F}$ | 2 | 1 | 1 | 0 |
| $\mathbf{G}$ | 1 | 2 | 1 | 0 |
| $\mathbf{M}$ | 1 | 1 | 2 | 0 |
| $\underline{\mathbf{Y}}$ | 1 | 1 | 0 | 2 |

* If both far-side destinations are the 18pt or higher, use $\underline{\mathrm{U}}$. the table, in order. Perfect!

After your swim, you crave a better view of some distant scenery.
Fortunately, you have binoculars, and voila!
Field Glasses Magnify Yosemite

Another option is "First Graders Memorize Yankee-doodle." (At least, they did when I was in school. "Yankee-doodle went to town...") With either mnemonic, the first word has one syllable, the second word has two syllables, and so on. If you don't care about the 1-2-3-4 syllabic scheme, choose one of the mnemonics below or create your own.

French Girl Massages You; Fairy Godmother Misses You; Fool’s Gold, Minimum Yield; Foolish Girls Marry Young; Far Gone, Many Years; Funny Guy, Master Yoda; Forest Green, Mustard Yellow; Flash Gordon’s Misspent Youth; Fancy Gadget Makes Yogurt; Fatigued Guests May Yawn; Funny Groucho Marx Yacks; Foster Grants Mystify You; Field General Must Yell; Fit Guy Mauls You; Forrest Gump Moons You; Frosty Glass Mirrors You.

When nactating any doublets move, you should, naturally, count the number of portions in each area. If it is uni-areal (a 4:0 ratio), use R (or U), D, J or I. If the move is bi-areal (2:2, $3: 1$ or $1: 3$ ), use a plain, underlined or dotted BEACON family (SZ inclusive).

If, on the other hand, the move is tri-areal (i.e., played in three areas and therefore a 2:1:1 ratio), I recommend you count the portions in each area (from back area to front) and translate it to a four-digit code-exactly as it appears in the table above.

For example, if there is 1 run, 0 downs, 2 jumps and 1 inside, think of it as "1021." With enough practice, you will instantly recognize that the corresponding letter for 1021 is M, but until that day comes you can adopt this two-step procedure:
(1) Ignore the 2 for a moment. Where is the 0 (zero) relative to the 1 s ? If the 0 is fiRst, use RDJI. If it is Flanked, use FGMY. If it is Final, use FGMY. (All three key words begin with " f ," but there is an R only in the first!

(2) Identify whether the 2-portion area is in first, second, third or fourth position. This tells you which letter of your (four-letter) sequence to use.

Returning to the example cited, your code is 1021. The 101 part (zero is Flanked) tells you that it must be one of the letters in the FGMY sequence, and the placement of the 2 in third position tells you to use the third letter of that sequence, which is M.

With practice, this two-step procedure will become second nature.

Positions \#90-93 (illustrated below) generate moves for all twelve 2:1:1 ratio families, plus $\underline{U}$ (a variant of the $\underline{R}$ family). To make this procedure easier to follow, I've included traditional notation and highlight. The " 0 " (zero) area is placemarked by green, both the " 1 " areas are colorless, and the portions in the " 2 " area are highlighted in yellow.


In \#90 (above), Black rolled 44. His three best moves (shown below) are all 2:1:1 ratios. How do we nactate them?

Below, left, the 90.1 move ( $24 / 20 / 16$ 9/5 6/2) has 2 runs, 0 downs, 1 jump and 1 inside, giving us a code of 2011. The 011 part (zero is fíㅗst) gives us the RDJI sequence. As 2 is in the first area, the first letter $\underline{\mathbf{R}}$ is the appropriate Nactation.
[For any 011 code (i.e., 2011, 0211,0121 or 0112 ), the 2-portion area tells you the letter: 2 Runs is $\underline{R}, 2$ Downs is $\underline{\mathrm{D}}, 2$ Jumps is J , or 2 Insides is $\underline{\mathrm{I}}$. Cool, eh?]

The 90.2 move ( $24 / 20(2) \quad 9 / 56 / 2$ ), also with a 2011 code, is solved the same way, except with neither far-side destination below the 18pt, you use the variant of $\underline{R}$, which is $\underline{U}$.

The 90.3 move, 24/20/16 13/9 6/2, has a code of 2101. The Flanked zero (101) signals the FGMY sequence. As the 2 is in the first area, you use the first letter, F. Catching on?


The (rather distant) fourth best move is $24 / 20$ (2) 13/9 6/2. It has the same 2101 code as 90.3 and is therefore in the same F family. That move (not diagrammed) is dealt the lower-case " f " because the owned 20pt is farther (than the owned 16 pt is) from the 6 pt .

Again, the two-step procedure is:
(1) Where is the zero (relative to the 1 s ):
físt ( 011 = RDJI), Flanked ( $101=$ FGMY $)$, or Final $(110=\underline{\text { FGMY }})$ ?
(2) Where is the 2 : in the first, second, third or fourth area?

Let's look at another batch of moves.


In position \#91 (above), Black rolled 33. How do we nactate his three best moves?
The moves shown in 91.1 (23/20(2) 13/10 9/6 ), 91.2 (23/20 13/10(2) 9/6), and 91.3 (23/20 13/10 9/6 8/5 ), respectively, yield codes of 2110, 1210 and 1120.

For all three codes, the 110 part (zero is Final) is the same, yielding a sequence of FGMY. For 91.1, the 2 is in the first position of its code; hence $\underline{F}$. For 91.2 , the 2 is in the second position; hence $\underline{\mathbf{G}}$. For 91.3, the 2 is in the third position; hence $\underline{\mathbf{M}}$.


Once again, the two-step procedure is:
(1) Where is the zero? $011=\underline{\text { RDJI, }}$, or $101=$ FGMY, or $110=\underline{\text { FGMY }}$.
(2) Where is the 2 : in first, second, third or fourth position?

Here is yet another batch of moves:

\# 92
41\$-64R-53U-51T-62P-32K-51-42E-21X-63R-61R-42Z-22

In position \#92 (above), Black rolls 22. How do we nactate his four best moves?

For $92.1(24 / 2213 / 11(2) \quad 6 / 4)$ and $92.2(24 / 22 \quad 7 / 57 / 56 / 4)$, respectively, we have 1201 and 1021. For both codes, the 101 part (zero is Flanked) gives us FGMY. For 92.1, the 2 is second; hence $\mathbf{G}$. For 92.2, the 2 is third; hence $\mathbf{M}$.

For 92.3 ( $13 / 11(2)$ ) $8 / 6$ 6/4) and 92.4 ( $13 / 117 / 5(2) 6 / 4$ ), we have respective codes of 0211 and 0121. For both, the 011 (zero is fiㄹst) gives us the RDJI sequence. For 92.3, the 2 is second; hence $\underline{\mathbf{D}}$. For 92.4 , the 2 is third; hence $\underline{\mathbf{J}}$.



Here is the final batch of moves:

\# 93 61P-62R-43Z-52H-21H-52E-52B-65s-63H-21U-11

In position \#93 (above), Black rolls 11. How do we nactate his three best moves?
For 93.1 ( $\square 11 / 107 / 66 / 5(2))$, 93.2 (23/22 7/6 6/5(2)), and 93.3 (23/22 11/10 6/5(2)), the respective codes are 0112 (zero is fiRst), 1012 (Flanked) and 1102 (Final), which yield respective sequences of RDJI, FGMY and FGMY. In each case, the 2 is in fourth position, corresponding to the fourth letter. That is, 93.1 is $\underline{\mathbb{I}}, 93.2$ is $\mathbf{Y}$, and 93.3 is $\underline{\mathbf{Y}}$.


Doublet moves with 2:1:1 ratios are the most difficult of all moves to nactate. Once you can handle these with confidence, you will be a true master of Nactation.

For reference, here again is the complete table of doublets:

## Table of Doublets

| Letter | Run | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{B}$ | 2 | 2 |  |  |
| S | 3 | 1 |  |  |
| Z | 1 | 3 |  |  |
| E | 2 |  |  | 2 |
| E | 3 |  |  | 1 |
| E. | 1 |  |  | 3 |
| A |  |  | 2 | 2 |
| A |  |  | 3 | 1 |
| $\mathbf{A .}$ |  |  | 1 | 3 |
| $\mathbf{C}$ | 2 |  | 2 |  |
| $\mathbf{C}$ | 3 |  | 1 |  |
| $\mathbf{C}$. | 1 |  | 3 |  |
| $\mathbf{O}$ |  | 2 | 2 |  |
| $\mathbf{O}$ |  | 3 | 1 |  |
| $\mathbf{O}$. |  | 1 | 3 |  |
| $\mathbf{N}$ |  | 2 |  | 2 |
| $\mathbf{N}$ |  | 3 |  | 1 |
| $\mathbf{N}$. |  | 1 |  | 3 |


| Letter | RUn | Down | Jump | Inside |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Q}$ | 1 | 1 | 1 | 1 |
| $\mathbf{R}^{*}$ | 4 |  |  |  |
| D |  | 4 |  |  |
| $\mathbf{J}$ |  |  | 4 |  |
| $\mathbf{I}$ |  |  |  | 4 |


| $\mathbf{R}^{*}$ | 2 | 0 | 1 | 1 |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{D}$ | 0 | 2 | 1 | 1 |
| $\mathbf{J}$ | 0 | 1 | 2 | 1 |
| $\mathbf{l}$ | 0 | 1 | 1 | 2 |
| $\mathbf{F}$ | 2 | 1 | 0 | 1 |
| $\mathbf{G}$ | 1 | 2 | 0 | 1 |
| $\mathbf{M}$ | 1 | 0 | 2 | 1 |
| $\mathbf{Y}$ | 1 | 0 | 1 | 2 |
| $\mathbf{F}$ | 2 | 1 | 1 | 0 |
| $\mathbf{G}$ | 1 | 2 | 1 | 0 |
| $\mathbf{M}$ | 1 | 1 | 2 | 0 |
| $\mathbf{Y}$ | 1 | 1 | 0 | 2 |

* R row: If all portions are played to the 18pt or higher, use the U family.
* $\underline{\mathrm{R}}$ row: If both far-side portions are played to the 18pt or higher, use the $\underline{\mathrm{U}}$ family.


## Section 17: Rollouts

I gratefully acknowledge Ken Bame and Mike Mannon for their tireless assistance in generating rollouts for this tutorial.

Diagrams for all positions in this tutorial, and the move sequences that reach them, are reproduced below. Beneath each one, rollout result(s) are represented by "nacbracs" (Nactation brackets). Within the brackets, the best moves (in bold red typeface) are listed in descending order of strength. After each individual move (except the first one), the error size is expressed in thousandths of a point (e.g., "12" means .012).

After the brackets, the blue typeface conveys some bot-related information along with the number of trials in thousands rounded down-e.g., 20736 trials is expressed as "20."

For example, the \#1 position (of the tutorial) is 54S-63R-31. The nacbracs [ $\mathbf{P}$ @87 H94 X101] "<=5 means: the best move is P (Point); the second, third and fourth best moves are @ (anchor), H (Hit) and X (hit and split), respectively, which have relative equities of $-.087,-.094$ and -.101 . Each of the moves is rolled out 5000+ times (5184, actually).

The above synopsis provides what you need to know (and then some) to glean the important information about the positions: the order and relative strengths of the moves. If you would like to read about nacbracs in greater detail, I recommend these posts:
http://www.bgonline.org/forums/webbbs_config.pl?noframes;read=111254 http://www.bgonline.org/forums/webbbs_config.pl?read=147386

\# 1 54S-63R-31
[P @87 H94 X101] ">=5

\#2 White's opening 52 [S D12 \$45] "+28*5
" $<31$ *5

\#3 White's opening 61
[P U227 S228 N248 T273 B297] ' ${ }^{6} 62$

61P-63 [R Z48 D105 \$107]
" $<=5$

\#4 White's opening 21
[\$ S8] "+46,
[\$ S8 U48 D51 V64] ~80*5
21\$-62 [S Z10 \& 13 \$21 D26 R28 U43] '<46**31

\# 7 51S-43
[U D2 S5 Z9 X12] " $\wedge 46 * * 3120$, [U...N43 T65] "<=5

\#10 54D-22
[E N34 H96] '<15*5

\#5 White's opening 43 [D Z3 S10 U23] "+46*12 7 43S-52 [S X42 \$66] "<=5

\# 8 43Z-32
[H X8] ' 446 ,
[H X4 K46] '<62*15 43Z-62 [H h314 X331 S348] ">=5

\#11 54S-55
[A N43 P59 J102] '<5
54S-33
[A C174 O175] "<=5

\#6 White's opening 43
[D Z3 S10 U23] "+46*12 7 43Z-51 [S X21 U33 \$45 D76] '<62*31 5

\# 9 51S-44
[B A23 E58 N83] '<31*10 g[A P70 N76 B109] "<=5

\#12 41\$-33
[C E4 B25] ' $146^{*} 5$,
[C...A60 U88] '<5

\#19 51S-51S-53P-53P-21
[U V6 S25 D51] "<=62*15 5

\#20 51\$-43S-42
[U V13 Z28 S50 c50]
'<62**15

\#15 51\$-51\$-31
[E N3 A16 C28 H72]

\#21 41\$-32S-63
[J C14 O46] '<62

\#25 65R-52S-43
[T H29 S61 X74] ' $<31^{*} 1515$
65R-52S-41
[T h150 S160 H167] ">=5
65R-52S-32 [T S21 K28 D63 H64 Z90 X106] '<31**5

\#28 N 62
[S Q1 R2 r11 V26 C64] "<103**20 10

\#23 21\$-52S-31
[I N19 E19 A42 C71 n84 O98] '<62***5

\#26 52D-63S-31P-31P-42
[L X18 H108] ">=31*5

\# 29 51S-41K-1-52V-21H-43H--63R-65H-31@-51T-51
[\$ \%1 U7 S30 269 R82 s93] $62 * * 10$

\#24 42P-53P-64S-22
[I @25 H27] ">=15

\#27 65R-53P-52D-64H--21H-43@-41
[W P18 U33 B67] ">=20*5

\#30 52S-32X-21H-42@-62X--54R-32@-52H-F-51T-51
[\$ \%10 S19 U63] ">=62*20 5

\#31 54D-66B-32
[ \& =E W6 U30 e39 c56 C68] "<=62**15 5

\# 34 62S-41X-65H-62H-32
[@ \#10 H46] '<62*15

\#37 65R-43Z-66
[D Z23 P26] '<31,
or [D U23 P26] by assumption
d[Z D7] '<62
s[Z D4] '<62
g[P D38] ' $<5$

[S Z10 \&13 \$21 D26 R28 U43] '<46**31

\# 35 52S-55A-??
(31^, 21< and 42> are forced fanning or entering moves)

\#38 64S-44
[R B19] '^25
or [R D19] by assumption
g[B E30 R57 C58] ">=5, or g[D 230 R57 458] ">=5 by assumption

\#33 21S-63R-21H-32@-65
[@ P23] '<62

\#36 64S-33D-11
[E. E14 Y50 y54] ' $<41 * 5$ or [I U14 \$50 L54] '<41*5 by assumption

\#39 43D-33
[C E19 R28 B29
H33 A53] '<62****10
or [...U28 B29 D33...] assumption d[C B2 E4 R7 H10 A21] "^62*15 s[E C3 B7] '<31
g[A C7 H43 E47 R63] " $<31 * 5$

\#40 65R-65R-65R-43D-
-53D-52P-65
[\$ H2 D36 \$64] ">=44
or [4 1-2 D36 264] ">=44 by assumption

\#43 65R-54S-62H-32H--41H-21H-31E-31
[I a8 A60] '<62*10 or [3 4-8 560] '<62*10

$\begin{array}{cc}\text { \#46 } & \text { 54S-43X-64R-64H- } \\ \text {-64H-62D-64 }\end{array}$
[R Z7 S14 K29 r37 k46 s74]

$$
\text { "<=62**10 } 5
$$

(similar to \#52)

\#41 65R-65R-65R-43D-53D-

$$
\begin{array}{r}
{[\text { P R11] ">=62 }} \\
\text { or [4 411] ">=62 }
\end{array}
$$


\#44 64P-62S-52S-11
[P O.4 n56 p62 N114] '<62*31 5 or [6 0-4 956 462...] '<62*31 5 by assumption

\#47 41S-61P-64P-61\$-32
[U S51 B113 V154]
< $=62 * 5$

\#42 62S-33
[D O17 N28 B95 E101] '<62**5 or [7517 328...] by assumption

\#45 21\$-64
[R Z304 U311 r327] ">=5

\#48 41S-61P-32
[U V232 s241 z261 8264 Z271 S287] ">=5

\#49 63S-51H-62H-31H-F--51P-41V-21K-5-21
[P p6] "<=62

\# 52 54S-43X-64R-64H--64H-61D-64
[Z R2 S5 r36 s72 z137]
" $<=62 * * 5$
(similar to \#46)

\#55 63S-62X-63H-64H-55S--64H-63R-43K-11E-
-51 [D C13 A15 c49 C76]
" $<=31 * * 5$
-42 [D a17 Z37 z42] "<=20*5

\# 50 21\$-51\$-31N-32C-64 [P p1] ">=62

\#53 63R-41S-51D-61H-43H--64H-51H-52P-42
[E N6 A51 P85 I86 O88]
"<=62*5

\# 56
...-51 [Z O168 c198 C216 C220] ">=5
...-42 [z N120 Z144 O161]
"<=5

\#51 N 53
[Z P12 z15 R41 Q41 r49 S58 U62] '<62**31**15

\#54 32S-63H-53H-61U--41P-F-64
[S s1 R7 Z24 S46 s50] "<=62**15 5

\#57 62S-61P-54@-11@-31P--61T-61N-31H-21H-61H--21H-54R-62K-F-61Z-22E-32
[E e19] " $<20$

\#58 43Z-43X-32H-42H-65R--55B-41-65R-22N-21U-51x--63R-22B-41U-55B-62@-
-43W-32r-42B-31H-61H-61D-32
[A C38 E49 J57 c77 a89 E110 e124 I144 e148...E327 E352] "<5

\#61 43Z-43X-44M-32-
-54N-11E-51R-51S-21
[R U9 V19 r32 R39]
" $<=62 * 20105$

\# 64 51S-41K-1-52V-
-31H-53S-42@-31
[P p54 S56 @65 s65
\$160 \#163] ">=5

$\begin{array}{ll}\text { \#59 } & \text { 63S-33 } \\ \text { [D O34 N51 R80 } & \begin{array}{l}\text { B87 H89] } \\ \\ \\ \end{array}<31^{* * 5}\end{array}$

\#62 64R-62X-F-52P--63R-62X-61H-42
[B Z22 S85] "<=15*5

\#65 65R-21\$-21\$-51N-22
[P G20 N87...p310
...p434...P523] ">=20*5 or [...D310...A434...I523]...

\#60 64P-54D-52S-52P--43R-63X-32@-52
[B C27 E28 R32 S48] '<31


$$
\begin{aligned}
\text { \# } 63 & \text { 51S-41K-1-52V- } \\
& -31 \mathrm{H}-53 \mathrm{~S}-63 \mathrm{U}-31
\end{aligned}
$$

[P H100 p107...@188...\#272]
"<=5

\#66 $\begin{gathered}\text { 61P-63R-64Z-41H- } \\ \\ \\ \text {-43H-61H-32H-31H- } \\ \\ \text {-63R-54K-51-22 }\end{gathered}$
[P p4 F70 B85...P191] " $<=62 * 5$

\#67 62S-52X-F-62
[H x29 h59 X70] '<62*15

\#70 64R-64S-33D-64R--21H-64H-63H-64H--21H-32H-32@-21
[L 11 P34 x50 H81 X88] or L B1... or d B1... "<<62*5

\# 73 32Z-41T-55P-65R-
-43R-21H-31B-32K-
-1-51D-32@-32
[\$ T28 \%48 \& 76 J84 D117 o117 D118 \$118] "<=10*5

\#68 $\begin{gathered}\text { 54S-63H-63H-64H-54 } \\ {[\mathrm{KK} \mathrm{k23]}]^{\prime}<31}\end{gathered}$
54S-63H-63H-64H-52 [k K12 @57] '<62*5

\#71 21\$-62S-61N-61H-61H--61H-52V-21K-3-64@--63C-65S-62H-61U-62P-52
[T t1 T24 t62] "<=62*15 5 or [D B1 O24 C62] " $<=62 * 155$

\#74 63R-21H-63U-41K-51--54K-31-53-51K-5-
-61U-21H-42@-63
[R R10 r10 r14 U17 S52]
<"62**41

\#69 $\begin{gathered}\text { 43Z-43X-42K-4- } \\ \text {-53H-5-42e-61U- } \\ \text {-31P-62@-61R-41 } \\ \\ \\ {[\text { L l19 X105] '<31*5 }}\end{gathered}$

\#72 64R-52D-62U-54K-32--61U-55P-41R-41S-32
[\$ \%4 \& 21 D21] "<=62*15

\# 75 N 41Q-21K-43-53@-21
[U u56 V67 u68 V75 v82 v112 U116] ">=5

\# 76 21S-64H-42H-64R-31P--64U-32K-4-52H-5-21
[P p32...p316...P520 P533 ...p601 P633 p673] "<=5 or A316 @520 D533 \#601 v633 0673

\# 79 64S-31X-62H-21H--F-43H-54-33
[A A. 23 M59 O68 J68 d81 D84 P91] ">=15*5

\#82 53P-53P-53S-53S--32X-F-11
[ N p4 E23] " $<=62 * 15$

\# 77 54S-62H-41H-61U-$-21 \mathrm{H}-61 \mathrm{H}-44$
[B E8 $\underline{\mathbf{Y}} 23 \underline{\text { M }} 38 \underline{\mathbf{f} 44 \text { C75] }}$ "<=62*15 125

\# 80 52S-43H-F-21p-55
[C M8 B18 \$57] ">=62*315

\#83 52D-21\$-43U-64H-52K-4--42H-41-62R-21x-53@-22
[Z S4 s5 z12 @23 F60 S70 s79]
"<=62***15 5

\#78 21S-53S-52H-62H--62K-51-43P-22E-22
[E Y19 A. 41 E.50] <=" $20 * 5$

\#81 52D-22N-55o.-66
[O C1 B30] "<=62*10

\#84 32D-63H-32H-42H-
-11E-61U-62O-42@--42S-53H-42H-F-64S--43S-51U-64K-21-33
[ $\mathbf{A}_{\underline{E}}^{\underline{E}}$ N6] "<=62

\#85 21\$-31H-32P-32R-31P--63R-32X-32H-54K-43--52@-52K-32-44
[C O1 g18 G20 B36 D75] " $<=62 * 20 * 5$

\#88 41\$-54S-32H-44E-53-55m--51-53R-55P-64D-42H-61H--64H-F-64P-53-21K-51-33
[Q q2 R89] "<=62*5

\# 91 52S-32X-55M-51-53Z-
-51H-65r-32H-41H-51V-659--64Z-F-65H-5-31P-22@-33
[G M7 F7 £24 g26 Z58 B65] <=62**15*5

\#86 51S-41K-31-F-65S-F--51S-43@-54R-55P-61U--31H-61H-52E-41K-32--42P-41O-65H-62K-32-11
[N. E. 11 A. 15 n.44] "<=31**5


## \#89 41S-63S-66P-43-62K-43--53-32K-43-22E-65R-64H--53@-31Z-42H-42H-22

[R U5 V11 B68] "<=62*31 5



\#87 32S-21X-41U-51H-53K--54-51H-54@-F-55B-
-21P-43R-64X-11Z-44C--51H-31H-53H-11E-22
[O. C. 3 M36 Y100] "<=62*5

\# 90 54D-62H-41H-63H-52V--32K-43-63@-65@-63P-52H--62U-51K-1-31P-51D-44
[ $\underline{R}=\underline{\mathbf{U}}$ F1 f54 E79 c80 C95] " $<=67 * * 5$


## \#93 61P-62R-43Z-52H--21H-52E-52B-65s--63H-21U-11

[Y I1 Y5 A. 31 E37 y61 y78]

## Section 18: Indexes

## Table of Contents

In the table below, the left-hand column lists the section titles (numerically). The middle column displays the beginning and ending (feature) diagram numbers for each section.

The right-hand column provides a character family when it is defined in that section for the first time. (Asterisks: * means non-doublets only; ** means doublets only.)

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\#1
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\#18-24
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\#29-35
\#36-39
\#40-44 0-9
D PR \$ S*
Z* U H X K
BEACON

V J I
T L W Q*
\% \& @ \# ^ < >

> \#45-52
\#53-58
\#59-62
\#63-73
\#74-76
\#77-87
S**EACON Z**E.A.C.O.N.
Q** $\underline{\text { U RDJI FGMY FGMY }}$

## Index of Terms and Concepts

Terms, concepts, conventions and rules for Nactation are listed alphabetically on the left. Corresponding section and/or diagram numbers are on the right.

Areal letters
Assumption
BSZ comparisons
Complex doublets
Convenience clause
Dedication clause (and playing through)
Down clause
Emboldenment (and colors)
Entering (or forced) portions
Family (hierarchy, ranking)
Fanning
Fewer blots convention
File names
Hit convention
Higher point sub-convention
Hit-more-6 rule
Home quadrant exception
Italics
Lower-case letters
Match score alternatives
More points convention
Movement areas (Run, Down, Jump, Inside)
Nacbracs
Nackgammon
Numerals
Portion (sub-move)
Ranking (hierarchy, family)
Rollouts
Rule subtleties and exceptions
Simple doublets
Slotting priority/rule
Style characters
Summary of conventions
Symbols
Tie-goes-to-the-inside-point directive
Which point convention
Wrinkle (outer board, farther from 6pt)
6pt convention
24pt-23pt (not counted as points) directive

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\#50-52
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## Index of Nactation Characters

The left column alphabetically lists Nactation letters, then symbols, then numerals. The second column gives the corresponding word. The third column supplies all diagram numbers for which the primary family member is captioned as a final-roll move.

| A | Attack or Aggress | $\begin{aligned} & \# 11,15.3,16.3,22.2,39.4,53.5,55.2,79.1 \\ & \underline{A} 84.3 \quad \text { A. } 86.3 \end{aligned}$ |
| :---: | :---: | :---: |
| B | Both | \#9, 17x, 17y, 39.3, 60.1, 62.1, 77.1 |
| C | Cross | \#12, 16.2, 39.1, 60.2, $80.1 \quad$ C $85.1 \quad$ C. 87.1 |
| D | Down ( $\rightarrow$ RDJI sequence) | \#2, 25y, 37.2, 38.2, 39.6, 55.1, 59.1 D 92.3 |
| $E$ | Each | $\begin{aligned} & \# 10,15.1,31.3,39.2,53.1,57.1,60.3,78.1 \\ & \underline{E} 84.1 \quad \text { E. } 86.1 \end{aligned}$ |
| F | $\rightarrow$ FGMY and FGMY | 90.3 F 91.1 |
| $G$ | $\rightarrow$ FGMY and FGMY | 92.1 G 91.2 |
| H | Hit | 8.1, 67.1 |
| I | Inside ( $\rightarrow$ RDJI sequence) | 23.1, 24.1, $36.1 \quad \underline{1} 93.1$ |
| J | Jump ( $\rightarrow$ RDJI sequence) | 21.1, 22.1 J 92.4 |
| K | Kill (hit twice) | 8.3, 46.3, 68.1 |
| L | Lift | 26.1, 36.4, 69.1, 70.1 |
| M | $\rightarrow$ FGMY and FGMY | 92.2 M 91.3 |
| N | Near | \#14, 15.2, 53.3, $82.1 \quad \underline{\mathrm{~N}} 84.2 \quad \mathrm{~N} .86 .2$ |
| $\bigcirc$ | Outer | \#13, 16.1, $81.1 \quad$ O $85.2 \quad$ O. 87.3 |
| P | Point | \#3, 33.2, 37.3, 49.1, 50.1, 63.1, 64.1, 65.1, 66.1, 76.1 |
| $Q$ | Quadruple split(non-doublets) <br> Quarters (doublets) | $28.1,51.5$ <br> 88.1 <br> R 90.1 |
| R | Run ( $\rightarrow$ RDJI sequence) | \#3, 38.1, 45.1, 46.1, 51.6, 60.5, 61.1, 74.1, 89.1 ^ |
| S | Split | \#5, \#6, 51.3, 52.3, 54.1, 60.4, 62.2; doublets 83.1 |
| T | sTack or Tower | 25.1, 25x, 70.3, 71.1 |
| U | Up | $\begin{aligned} & \text { \#7, 18.1, 19.1, 20.1, 36.2, 37.1, 39.5, 47.1, 48.1, } \\ & 51.4,61.4,75.1,89.2 \underline{U} 90.2 \end{aligned}$ |
| V | Variant Up | 18.2, 19.2, 20.2, 47.2, 48.2, 51.5, 61.5, 75.2, 89.3 |
| W | Wild | 27.1, 31.2 |
| X | Xplit (hit and split) | 8.2, 67.3 |
| Y | $\rightarrow$ FGMY and FGMY | 93.2 Y 93.3 |
| Z | Zplit (reverse split) | \#6, 51.1, 52.1, 54.5, 55.3, 62.3; doublets 83.3 |


| \$ | Slot | \#4, 29.1, 32x, 36.3, 72.1, 73.1 |
| :---: | :---: | :---: |
| \% | alternate slot | 29.2, 72.2, 73.2 |
| \& | double slot | 31.1, \#32 |
| @ | anchor | 33.1, 34.1, 63.3, 64.3, 66.2 |
| \# | alternate anchor | 34.2, 63.4, 64.4 |
| $\wedge$ | fan | 35x |
| $<$ | enter one checker | 35y |
| $>$ | enter both/all checkers | $35 z$ |
| 0 | 0pt, 10pt or 20pt | 44.2 |
| 1 | 1 pt , 11pt or 21 pt | 40.2 |
| 2 | 2 pt , 12pt or 22pt | 40.3 |
| 3 | 3 pt , 13pt or 23pt | 42.3, 43.1 |
| 4 | $4 \mathrm{pt}, 14 \mathrm{pt}$ or 24 pt | 40.1, 41.1, 43.2, 44.4 |
| 5 | 5 pt or 15pt | 42.2, 43.3 |
| 6 | 6 pt or 16pt | 44.1 |
| 7 | 7pt or 17pt | 42.1 |
| 8 | 8pt or 18pt |  |
| 9 | 9pt or 19pt | 44.3 |

In the darkly shaded column to the left of the text area of this document, click on the top icon. "Page thumbnails" provides you with an easy way to instantly jump to any page (though this tutorial is not actually cross-referenced by page number).

Now click on the second icon ("Bookmarks"), which displays three sub-icons. Click on + to expand, - to diminish. "Part 1" and "Part 2" let you navigate by section number, and "Nactations" by character segment. (To adjust the width of the column, drag the border or click on the right arrow at the top; and to restore, use the left arrow.)

